

# Mechanism Reduction for the Formation of Secondary Organic Aerosol for Integration into a 3-D Air Quality Model

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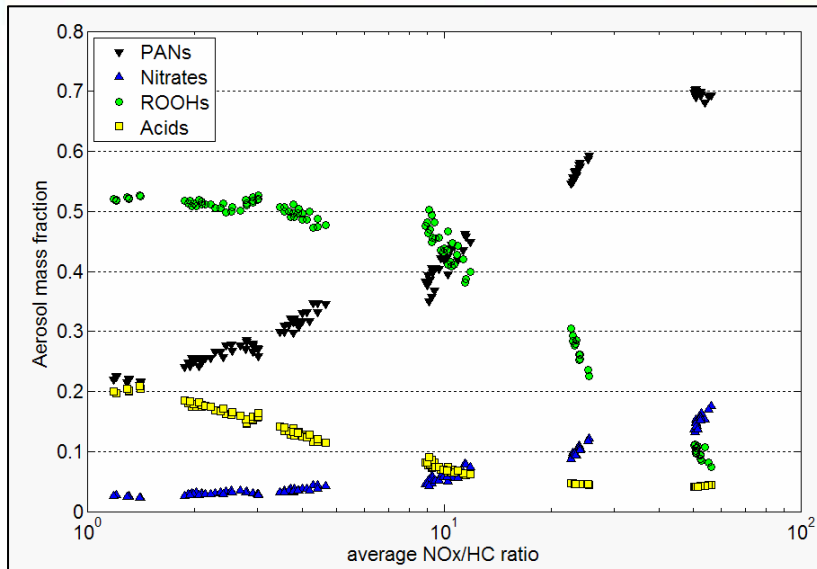
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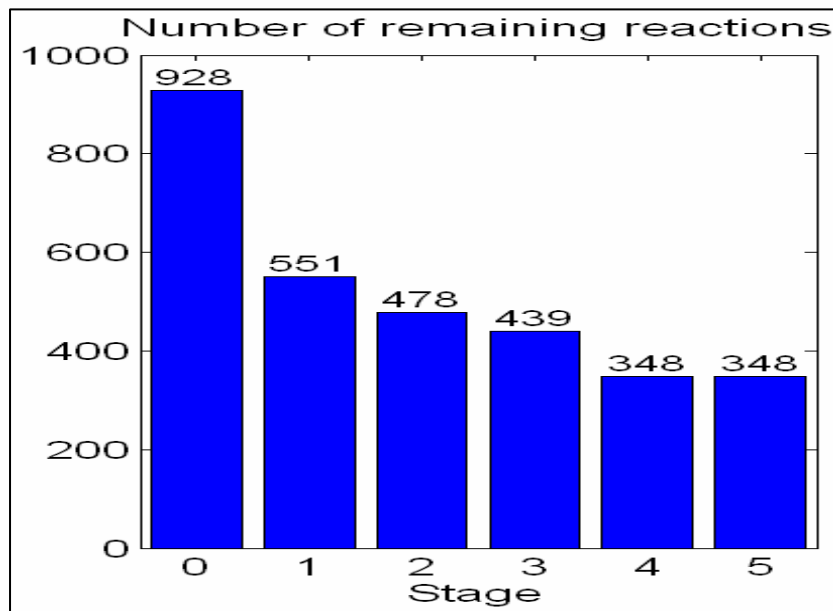
# Objective

To obtain an **accurate & simple chemical mechanism** for the formation of secondary organic aerosol (SOA) and ozone in a 3D air quality model

# Outline



**Part I**  
**Detailed mechanism (MCM)**  
for SOA formation



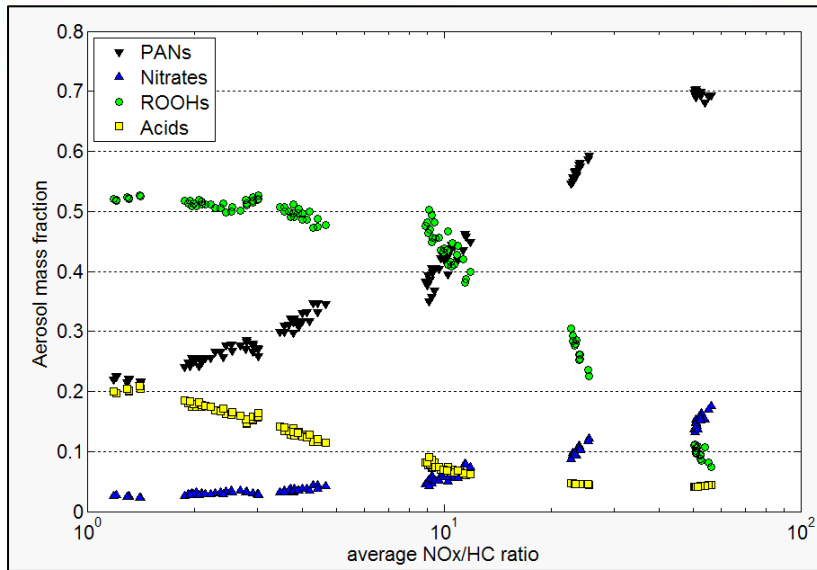
**Part II**  
**Systematic reduction of**  
the detailed mechanism

# Introduction

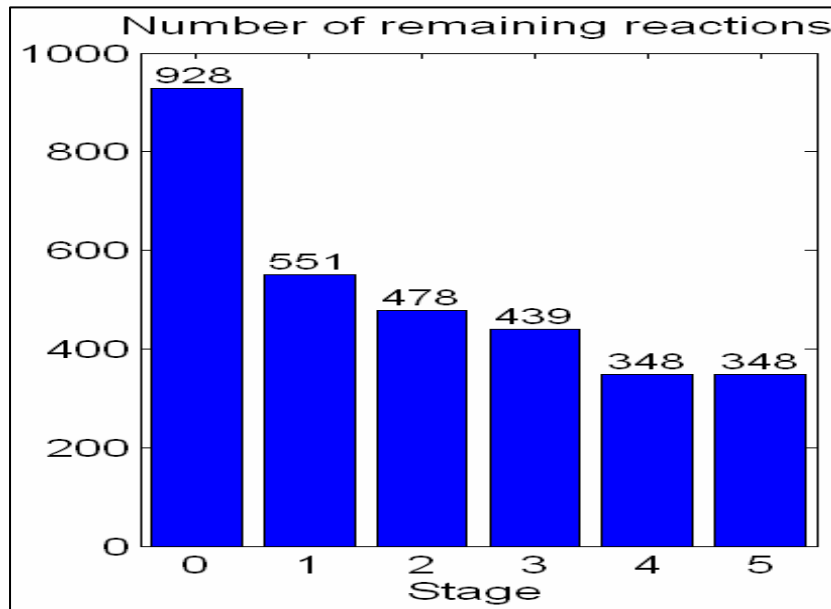
## Chemical mechanisms for 3D Air Quality Models

- ❑ Most chemical mechanisms were developed primarily for ozone formation, not for SOA
- ❑ MCM can be a candidate, but too **expensive**
- ❑ Some simplified mechanisms for the SOA formation, such as MAM (Mainz Alpha-pinene Mechanism), are available, but no methodology
- ❑ **Systematic reduction techniques** are required to reduce the mechanism under a wide range of conditions.

# Outline



**Part I**  
Detailed mechanism (MCM)  
for SOA formation



**Part II**  
Systematic reduction of  
the detailed mechanism

# Model Settings for SOA formation

## 1. Chemistry (MCM v3.1 from <http://mcm.leeds.ac.uk/MCM/>)

$\alpha$ -pinene oxidation	Inorganic	Organic	Total
Number of species	21	310	331
Number of reactions	48	928	976

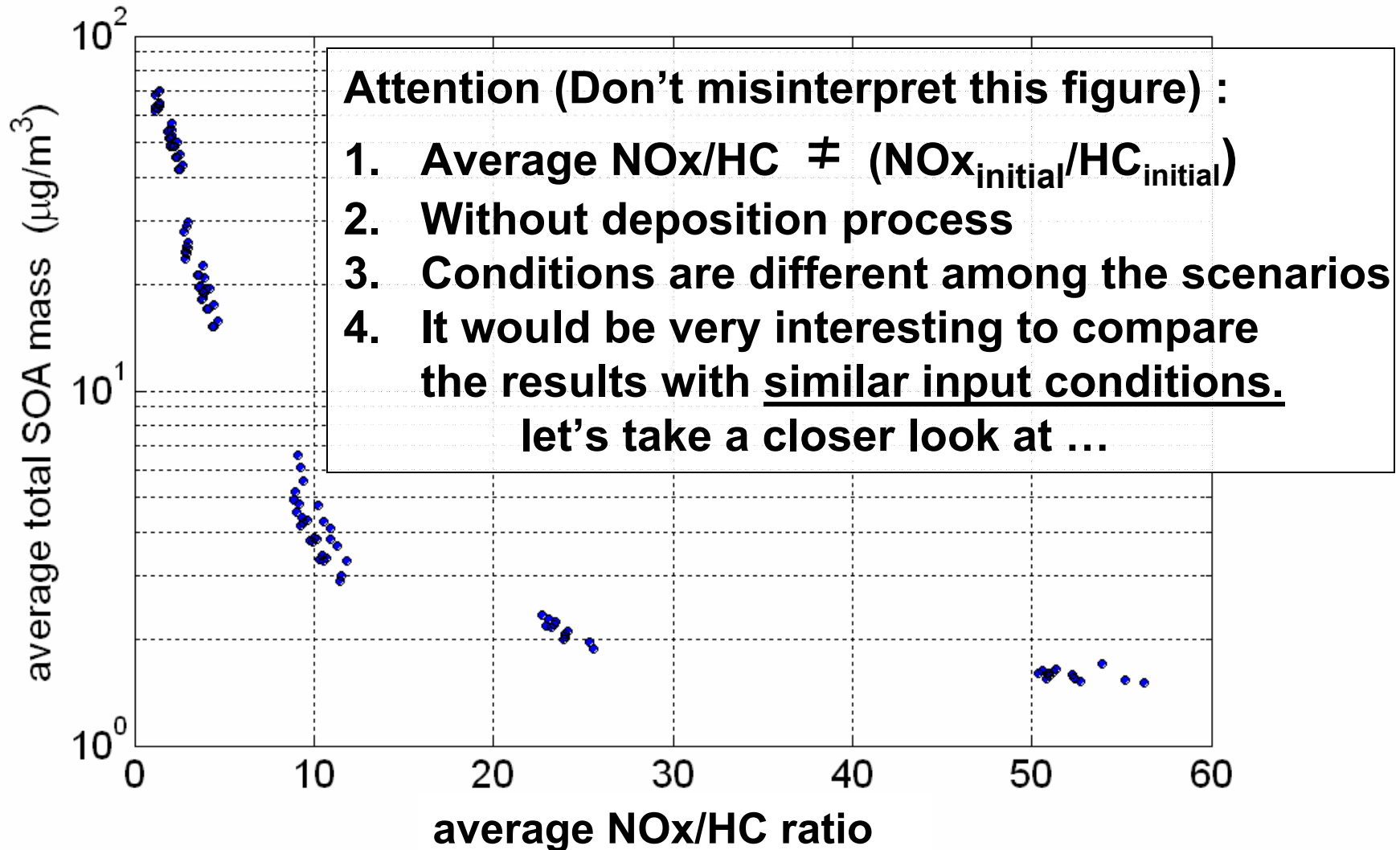
## 2. Model settings (108 selected scenarios—wide range of NO<sub>x</sub>/HC)

- 0-D box model coupled with G/P partitioning process
- Different emission rates and initial concentrations
- Diurnal variations of temperature and RH
- Without deposition

## 3. Hourly data points from last two days (**48 time points**) are selected for data analysis

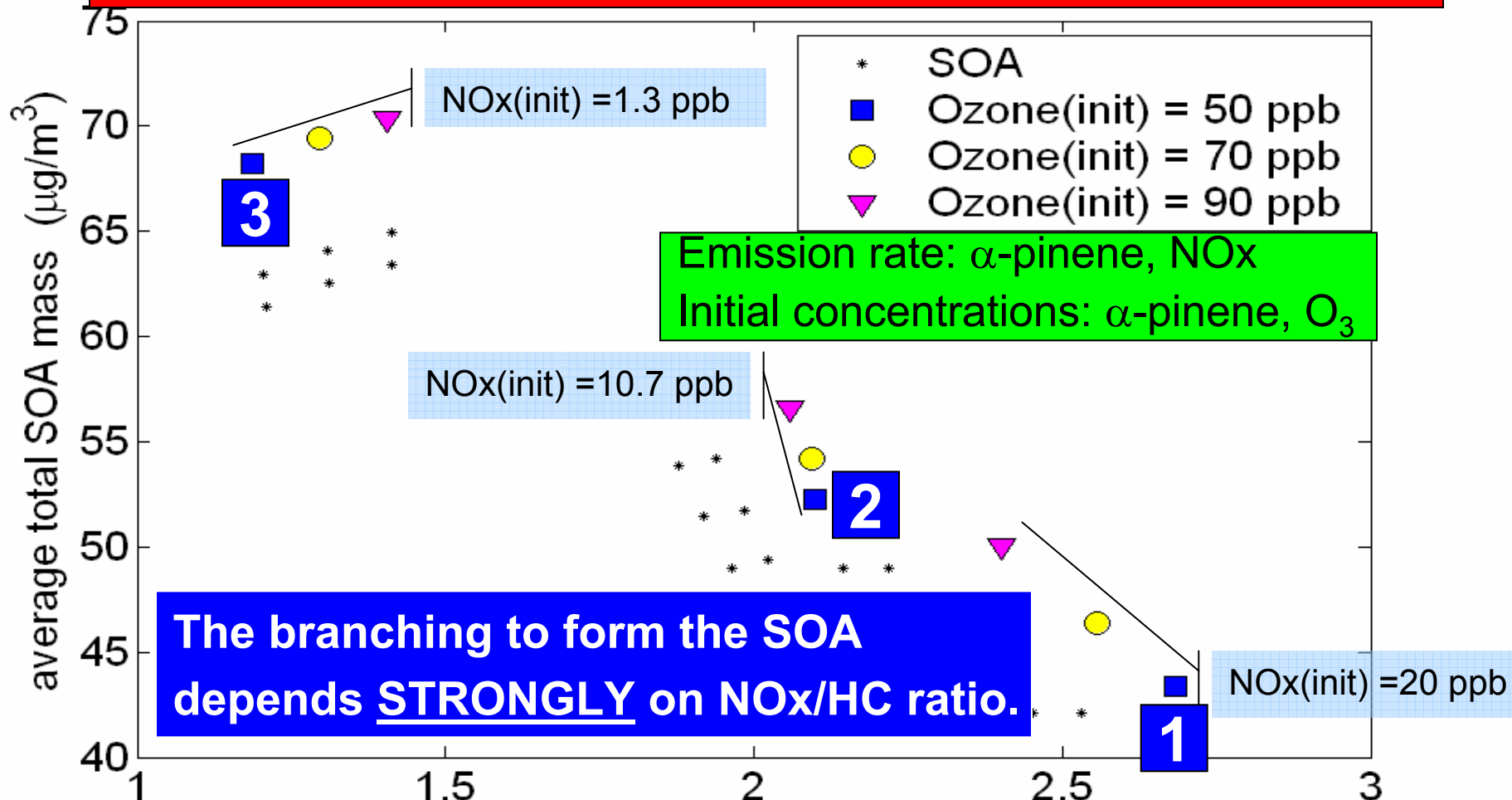
# Model results of the full mechanism (1/3)

## Summary of the 108 selected scenarios



# Model results of the full mechanism (1/2)

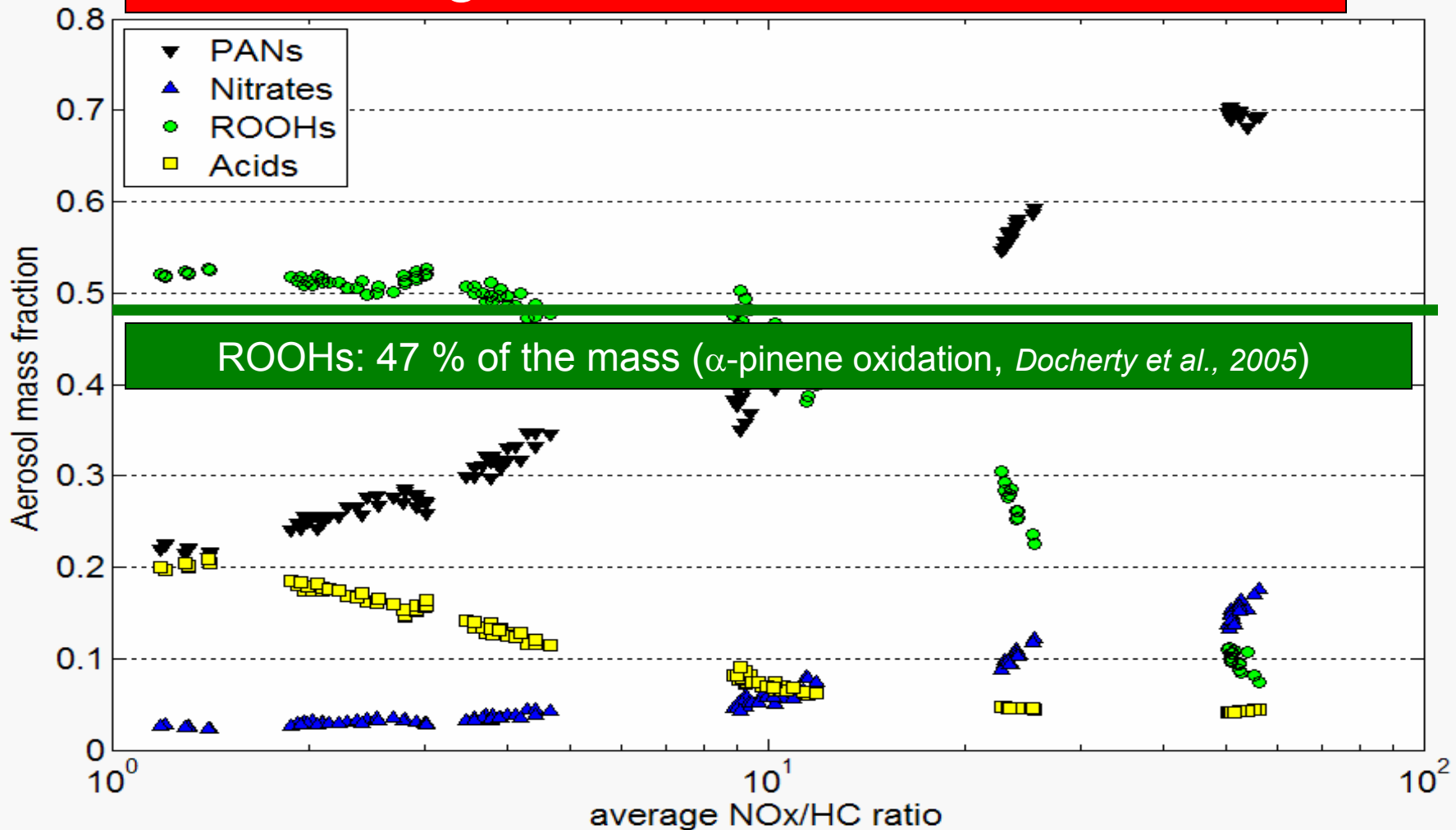
## Total SOA mass changes with the NO<sub>x</sub>/HC



High NO<sub>x</sub>  $\Rightarrow$  products are more volatile  $\Rightarrow$  less SOA

# Model results of the full mechanism (2/2)

## Organic aerosol mass compositions change with the NO<sub>x</sub>/HC ratio



# 28 important condensable compounds (1)

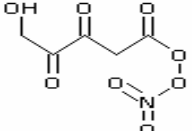
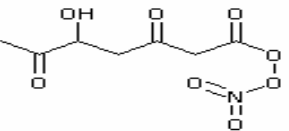
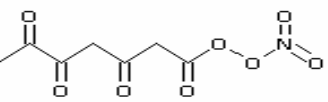
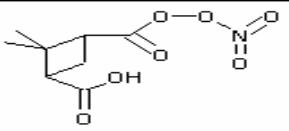
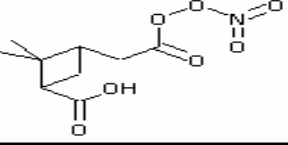
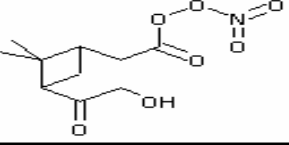
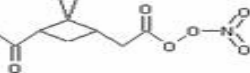
## 14 R-O-OH

C719OOH		609	C812OOH		615
C813OOH		635	C921OOH		622
C922OOH		642	C97OOH		573
C98OOH		597	NC1020OH		643
C106OOH		594	C107OOH		570
C108OOH		594	C109OOH		577
NAPINAOOH		570	NAPINBOOH		570

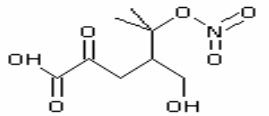
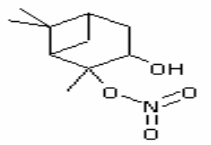
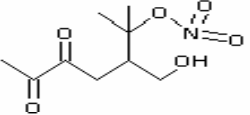
Boiling point (K)

# 28 important condensable compounds (2)

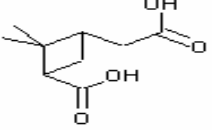
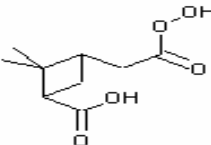
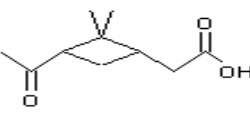
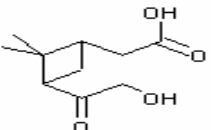
## 7 PAN

H1C23C4PAN		601	H3C25C6PAN		615
C7PAN3		604	C721PAN		609
C811PAN		621	C920PAN		628
C10PAN2		580			

## 3 NO3

C813NO3		640	APINANO3		559
C98NO3		603			

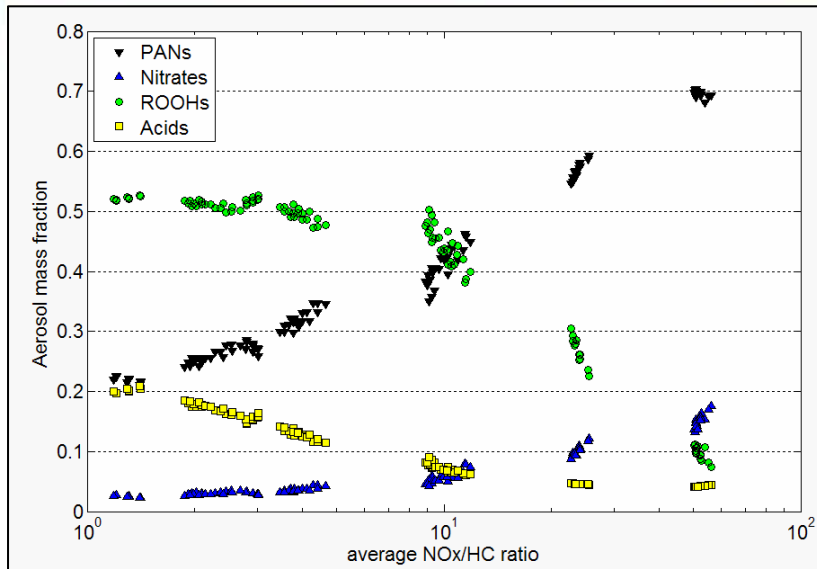
## 4 Acid

PINIC		612	C811CO3H		602
PINONIC		569	HOPINONIC		619

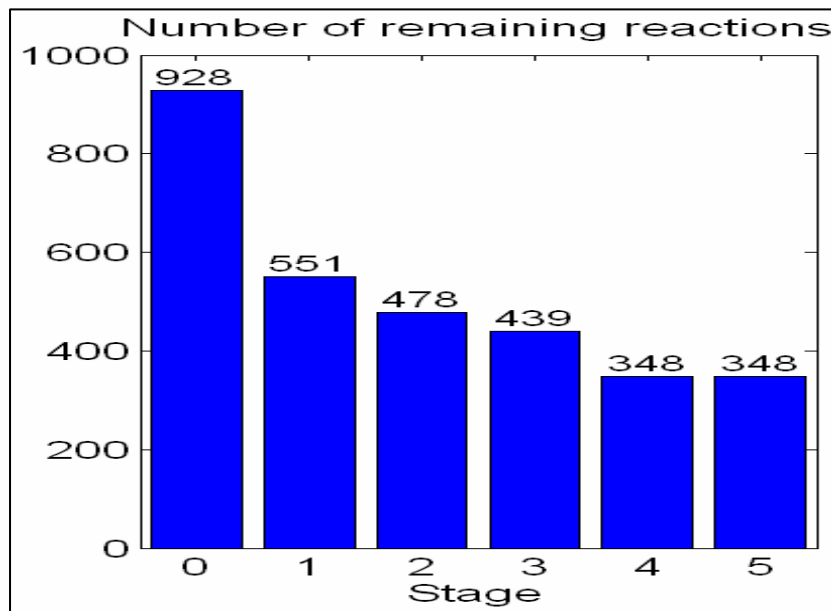
# Summary of SOA formation from MCM

1. Based on a detailed  $\alpha$ -pinene oxidation scheme, **total SOA** formed is **NO<sub>x</sub>/HC dependent**, and **more SOA** is formed at **low NO<sub>x</sub>/HC**.
2. The **organic aerosol mass compositions** also change with the NO<sub>x</sub>/HC—the group of **ROOHs** is the **dominant** one at **low NO<sub>x</sub>/HC**.

# Outline



**Part I**  
Detailed mechanism (MCM)  
for SOA formation



**Part II**  
Systematic reduction of  
the detailed mechanism

# Part II

## Mechanism reduction techniques

**Goal: remove unimportant species and reactions**

**Five stages:**

1. DRG or DRGEP method ???
2. Principal component analysis (PCA)
3. Quasi-steady-state assumption (QSSA)
4. Iterative screening method (ISSA)
5. Linear lumping



**Similar to rightsizing of a large company**

# Rightsizing of a large company

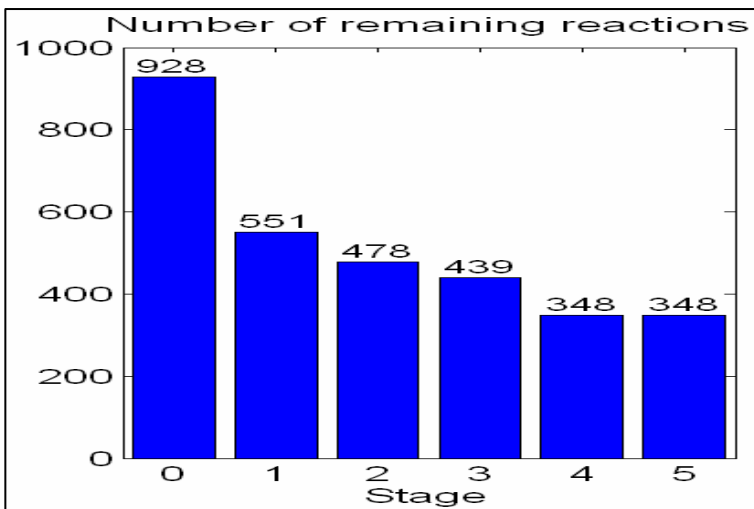


**Goal:**  
remove redundant people  
& departments/projects

**Results:**

People remained:  
**Important people  
necessary people**

# Mechanism reduction



**Goal:**  
remove redundant  
species & reactions

**Major  
species**

Species remained:  
**Important species  
necessary species**

# 1: Directed Relation Graph (DRG) (Lu and Law 2005, 2006)

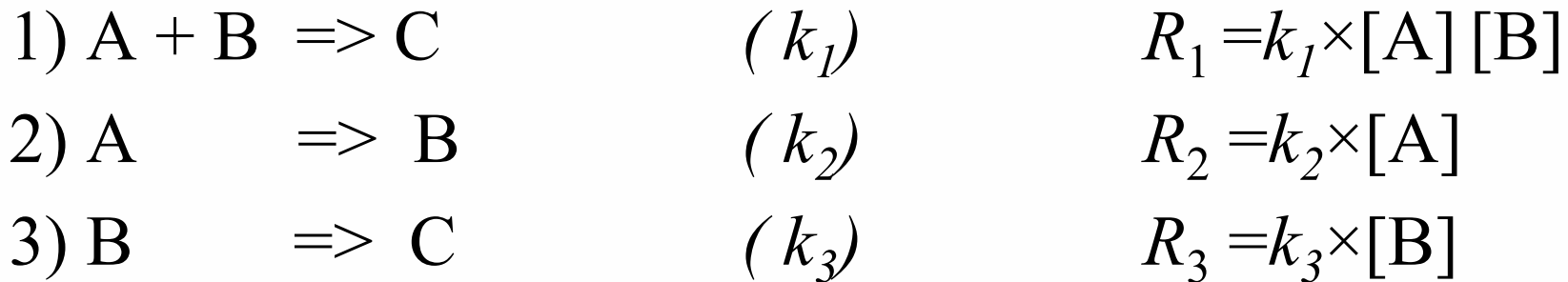
Contribution coefficient ( $r_{AB}$ )

**Species contribution**

$$r_{AB} \equiv \frac{\sum_{i=1, N} |v_{A,i} R_i \delta_{B,i}|}{\sum_{i=1, N} |v_{A,i} R_i|}$$

$v_{A,i}$  : Stoich. coef. of **A** in *i*th rxn  
 $R_i$  : Reaction rate of *i*th rxn  
 $\delta_{B,i}$  = 1 if **B** is a reactant in *i*th rxn

**Example:**



**Max( $r_{AB}$ )**

$$r_{AB} = \frac{|1 R_1| \times |1| + |1 R_2| \times |0| + |0 R_3| \times |1|}{|1 R_1| + |1 R_2| + |0 R_3|}$$

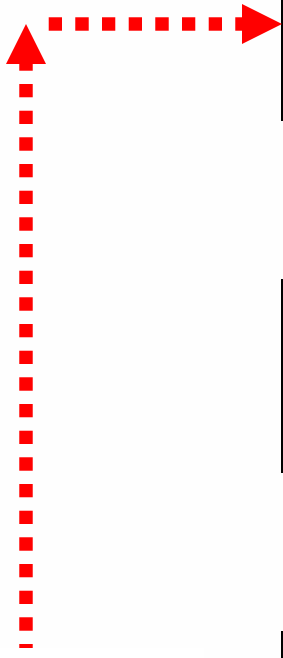
# 1: Directed Relation Graph (DRG)

Procedure to find “major species”

major species (A)

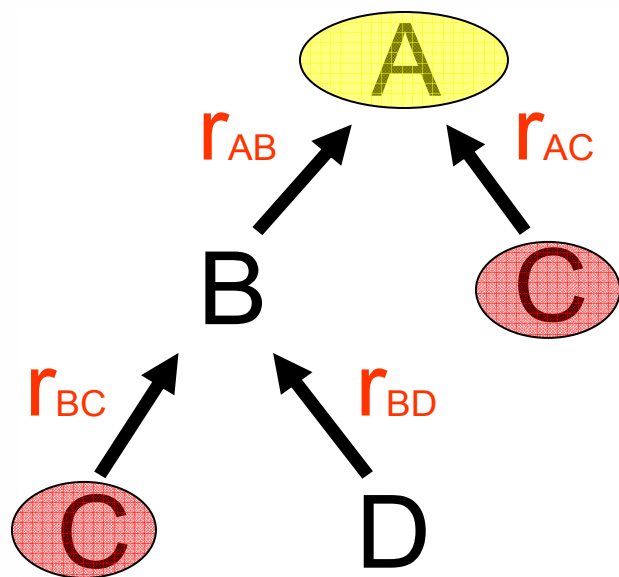
$$r_{AB} \geq \varepsilon \text{ (Threshold)}$$

Update major species  
(B becomes a major species)



# 1: DRG with error propagation (DRGEP)

(Pepiot and Pitsch, 2005)



**Path-dependent coefficient:**

Path #1: **C** → A       $r_{AC}$

Path #2: **C** → B → A       $r_{AB} \times r_{BC}$

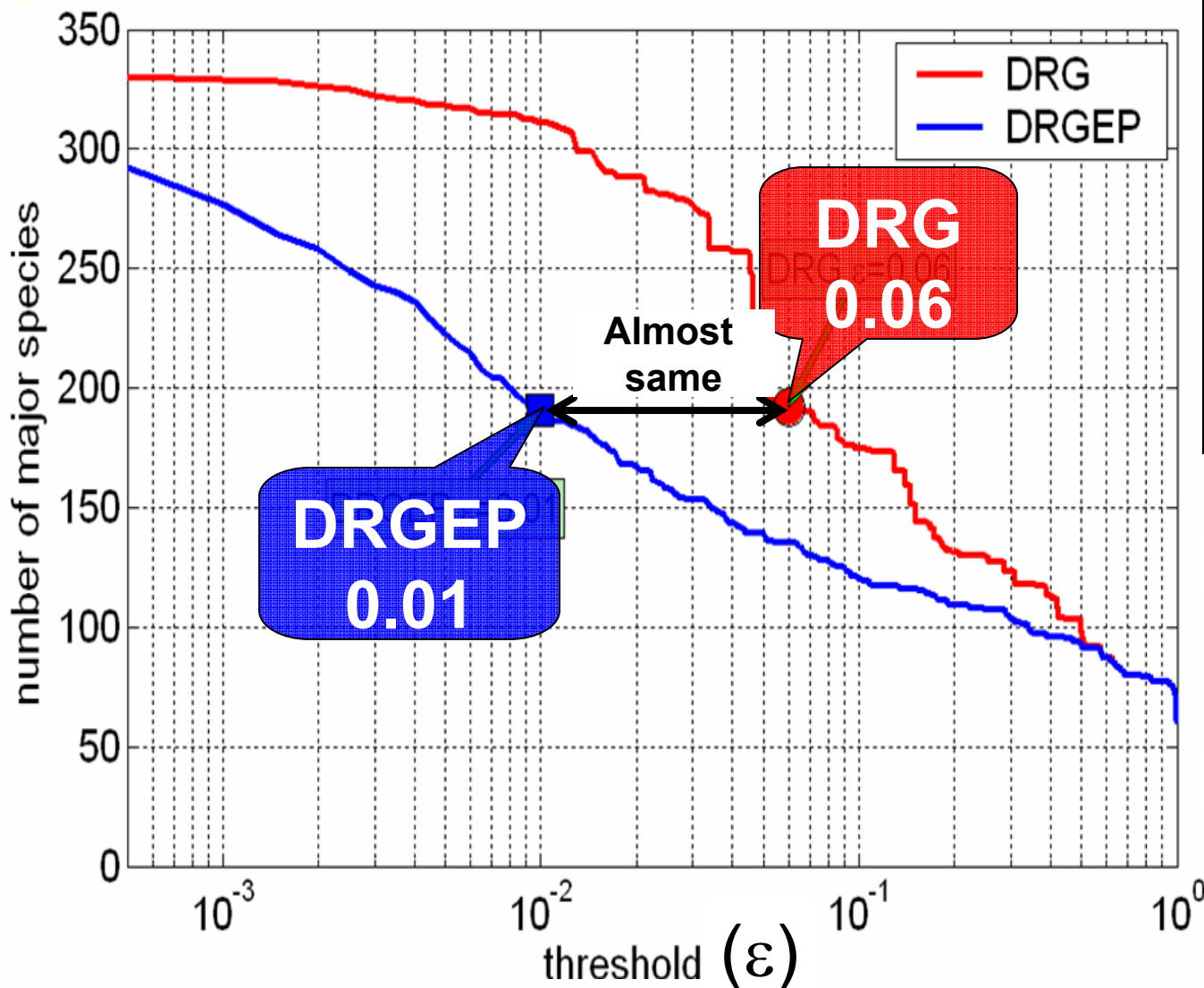
**Generalized contribution coefficient**

$$R_{AC} = \max\{r_{AB} \times r_{BC}, r_{AC}\}$$

In fact,  $R_{AC}$  is the *maximum* of all Paths from **C** to **A**.

**Procedures:** If  $R_{AC} \geq \varepsilon$  (**given threshold**), then **C** is a “*major species*” and retained in the mechanism. **No Iteration.**

# 1: Comparison between DRG & DRGEP

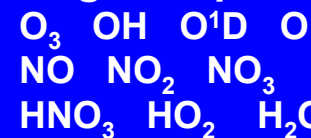


**39 important species:**

**1**  $\alpha$ -pinene

**28** condensable species

**10** inorg. compounds



All inorganic species are kept

**Species removed**

**DRG: 139**

**DRGEP: 140**

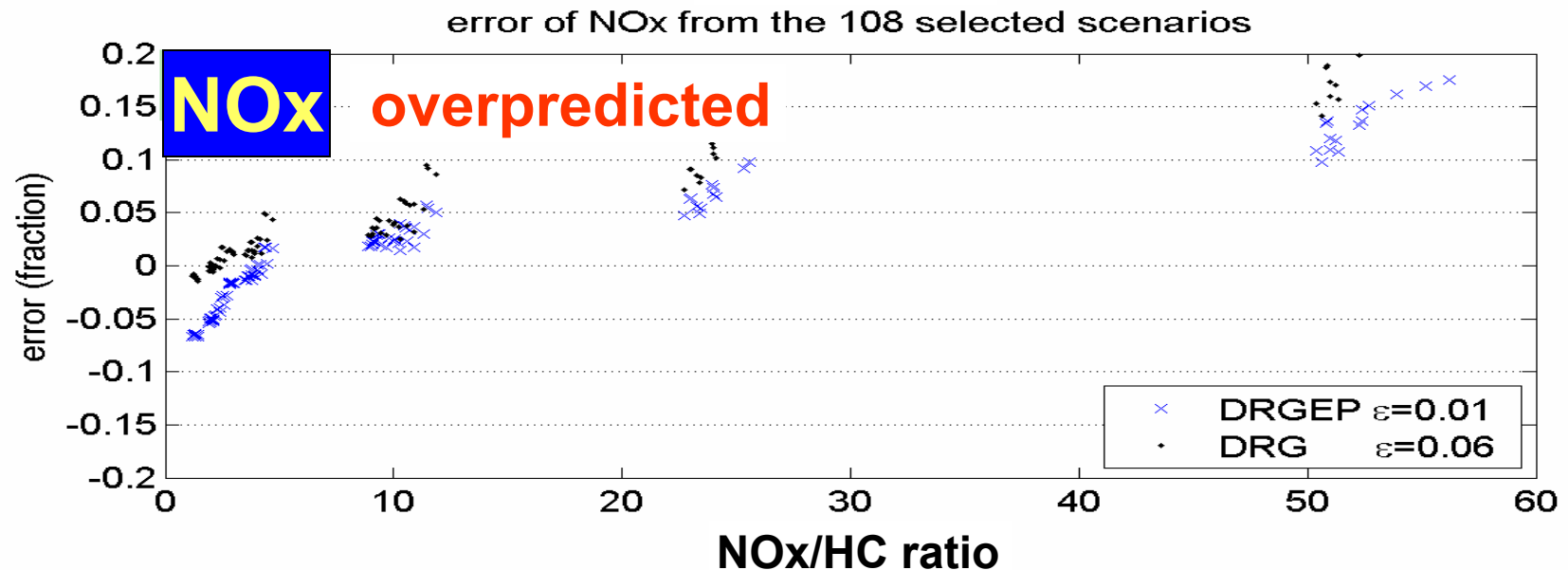
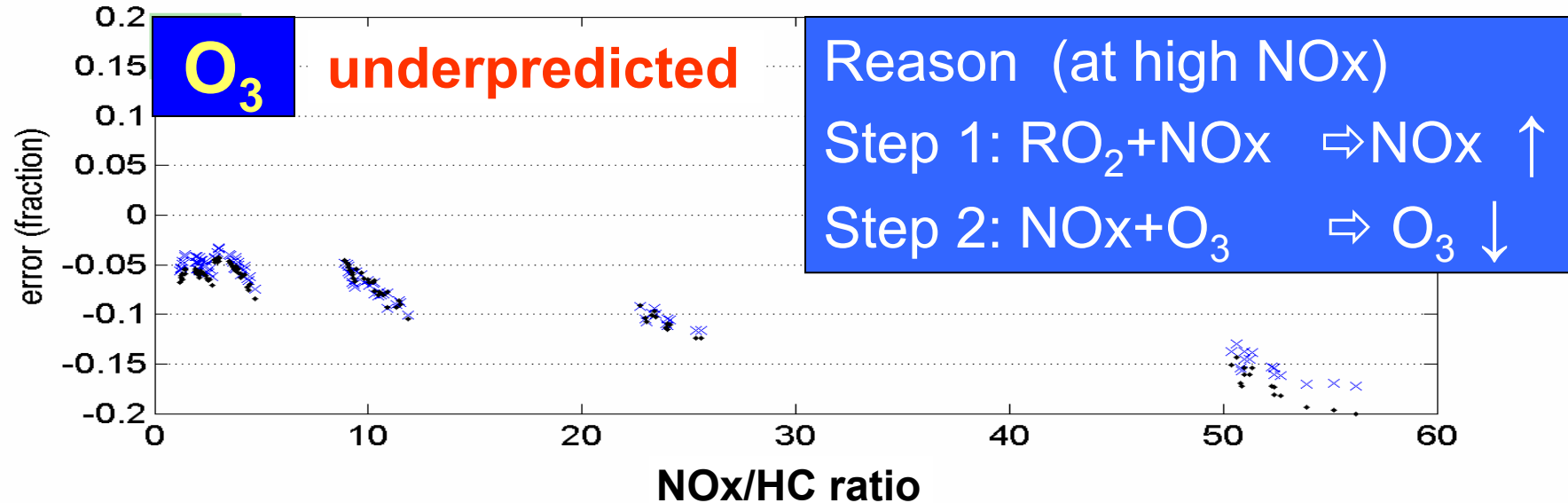
**Rxns removed**

**DRG: 387**

**DRGEP: 377**

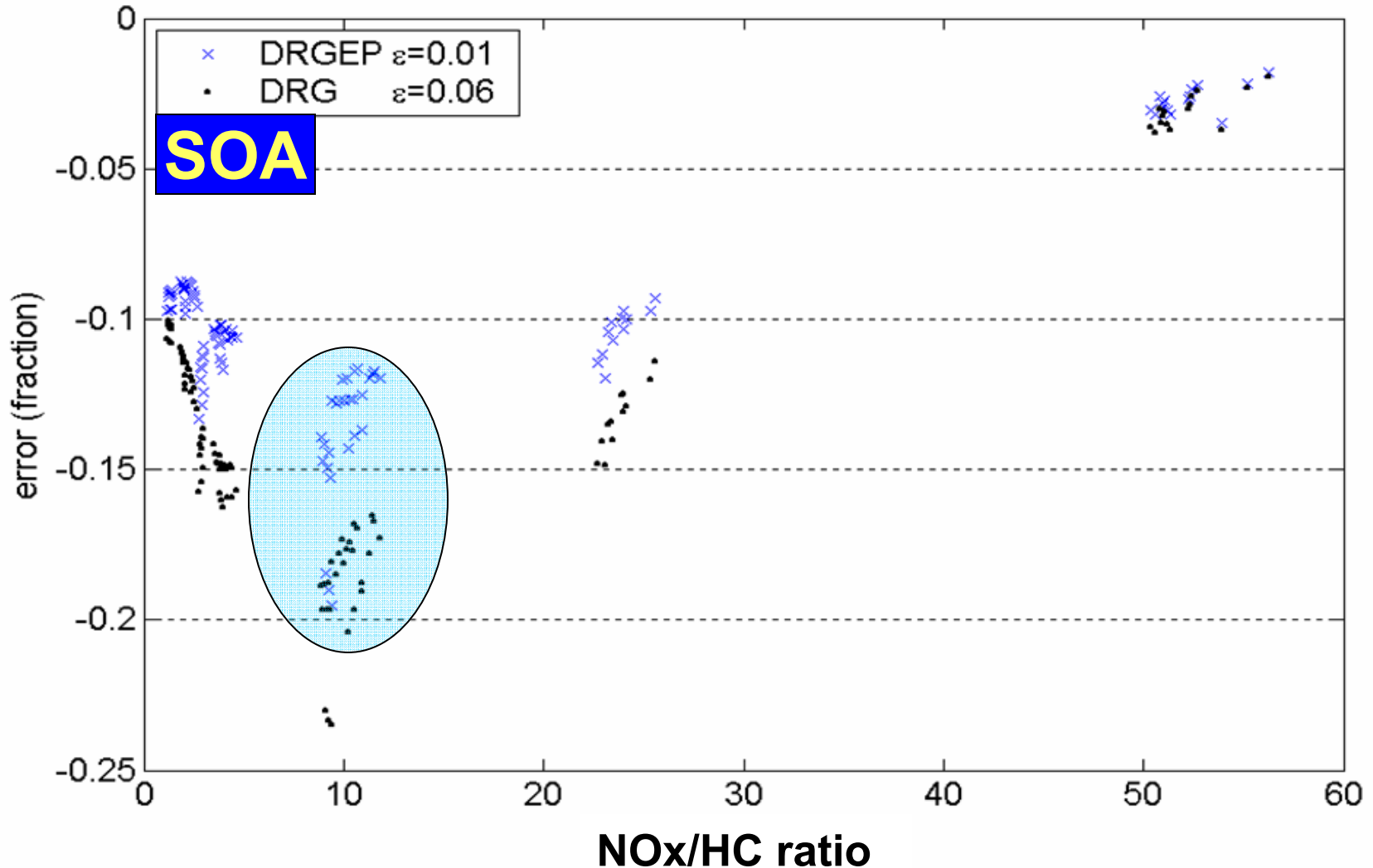
# 1: Comparison between DRG & DRGEP

error of  $O_3$  from the 108 selected scenarios

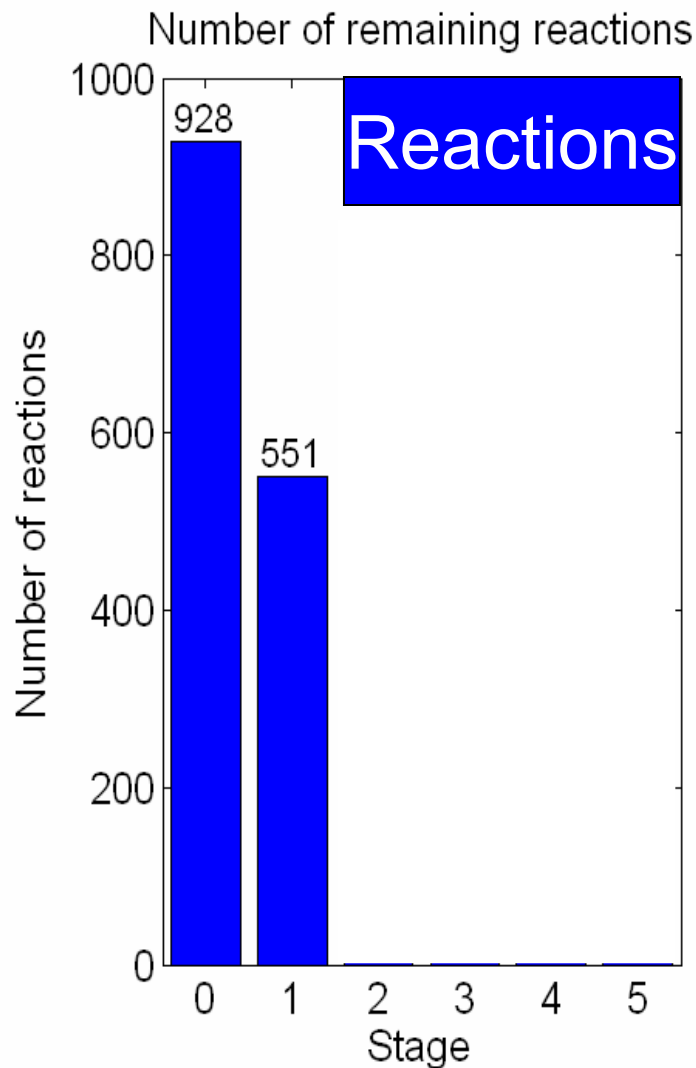
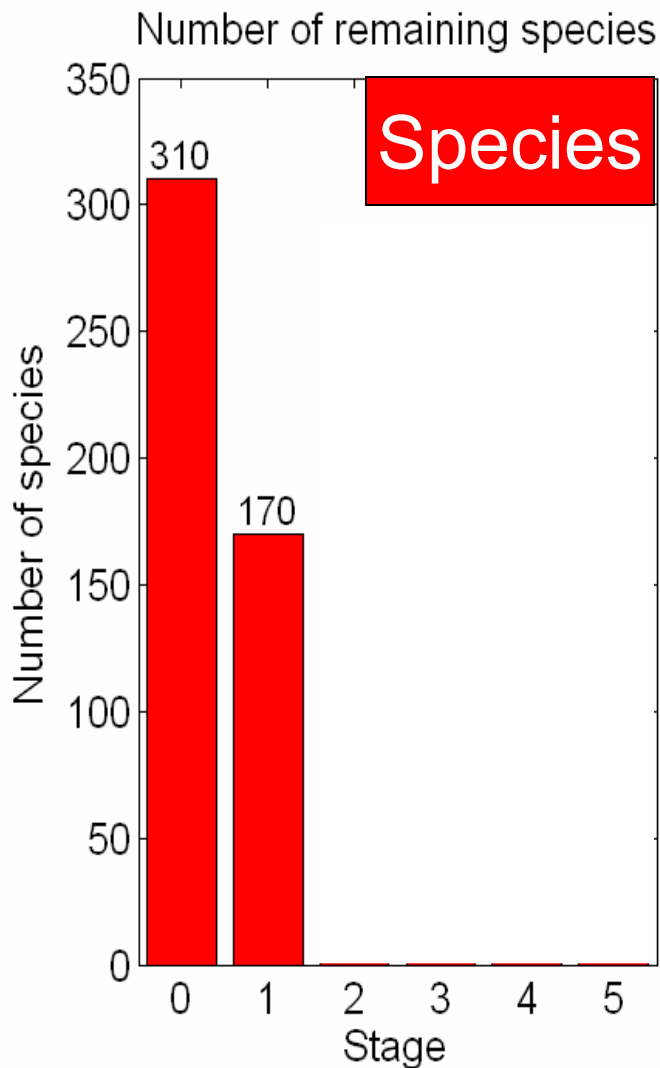


# 1: Comparison between DRG & DRGEP

**DRGEP is better than DRG in predicting total SOA**



# Summary of model reduction (1)



Stages:  
0) Full  
1) **DRGEP**

Removed:  
Species : 140  
Reactions: 377

# 5: Linear lumping method

*(This work)*

**Fixed fraction**

## 1. Question

- To determine whether two species can be lumped

# 5: Linear lumping method

## 2. Analysis

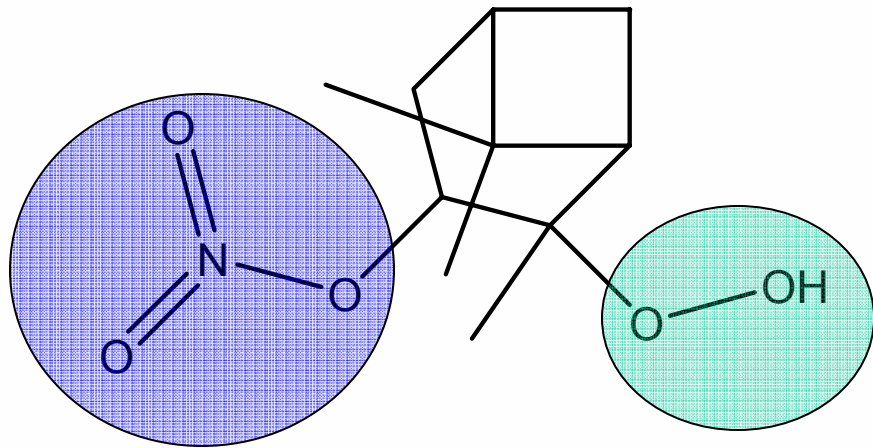
*(Huang et al. 2005)*

If **A1** and **A2** can be lumped, according to the linear lumping (**A=A1+A2**, **mixing ratio**), then

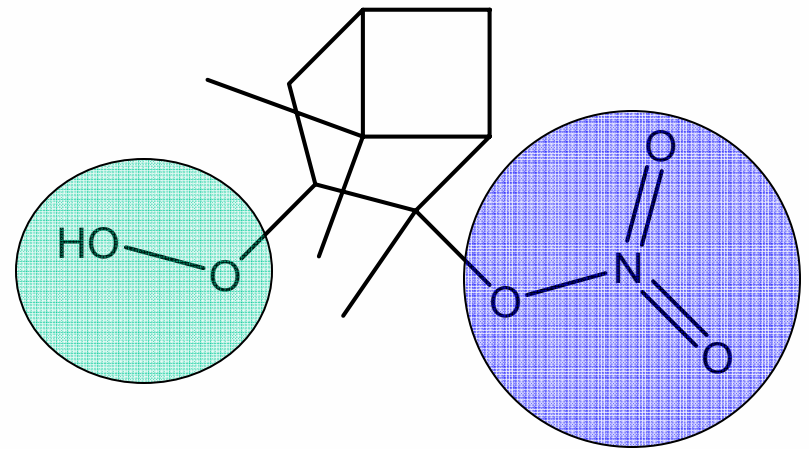
$$\begin{pmatrix} A1 \\ A2 \end{pmatrix} = (A1 + A2) \begin{pmatrix} \frac{A1}{A1 + A2} \\ \frac{A2}{A1 + A2} \end{pmatrix} = A \begin{pmatrix} \frac{A1}{A1 + A2} \\ \frac{A2}{A1 + A2} \end{pmatrix} = A \begin{pmatrix} x \\ 1 - x \end{pmatrix}$$

If  $x$  is almost a **fixed value**, then the two species can be lumped. We need to determine the **X**.

# 5: Two selected compounds



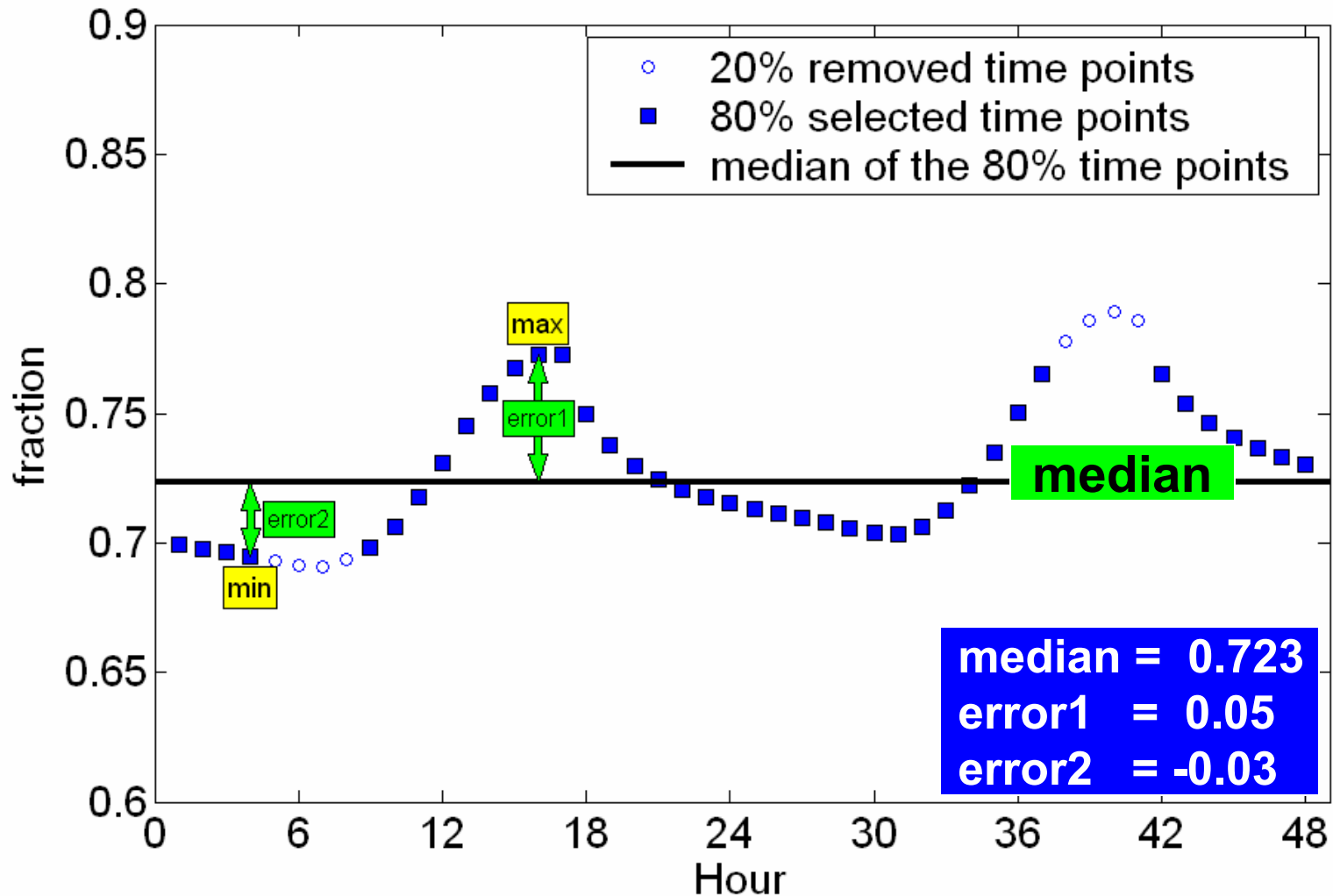
**NAPINAOOH**



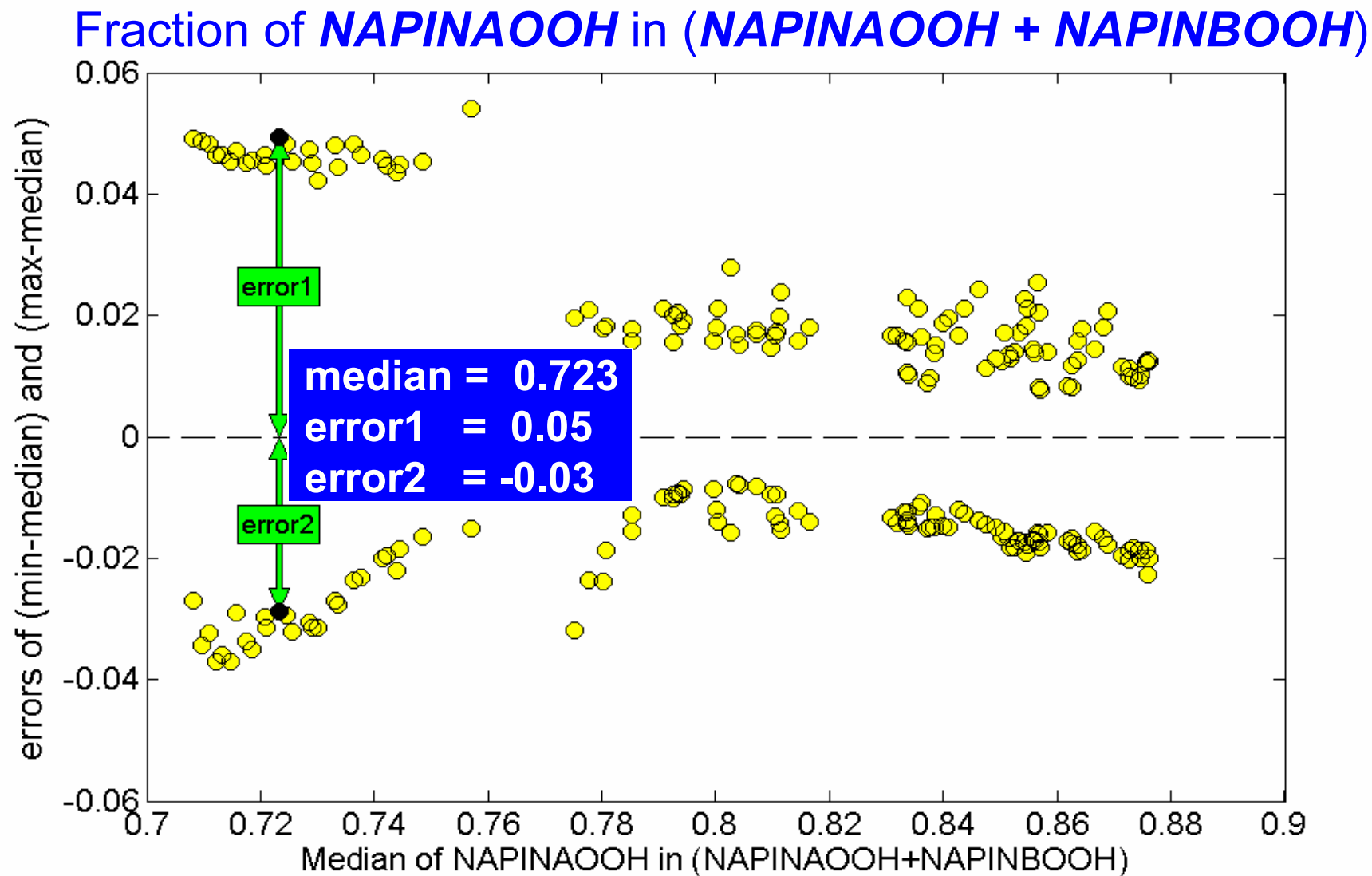
**NAPINBOOH**

# 5: Fraction (gas phase) from one scenario

Fraction of *NAPINAOOH* in (*NAPINAOOH* + *NAPINBOOH*)

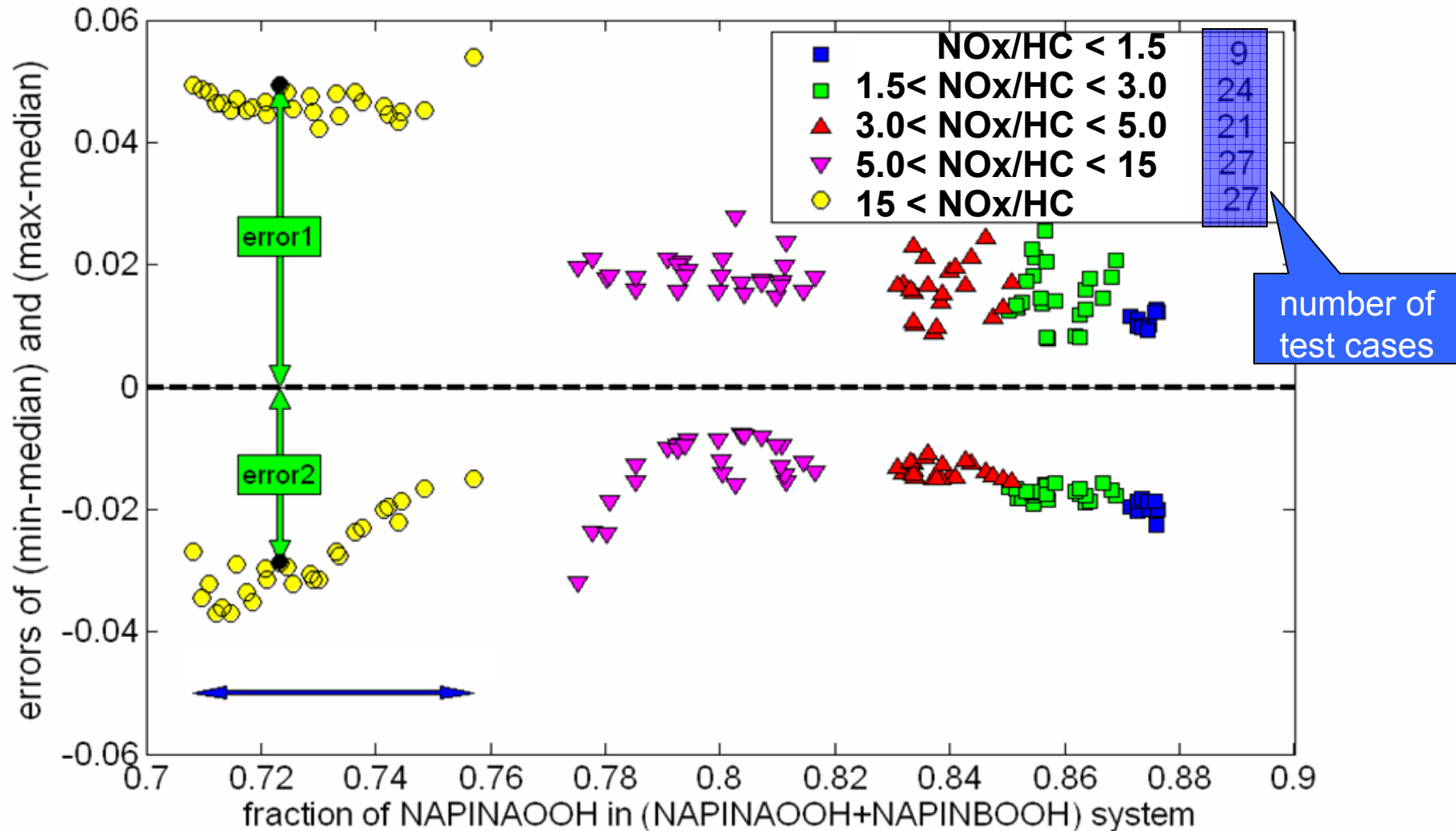


# 5: Fraction (gas phase) from 108 scenarios

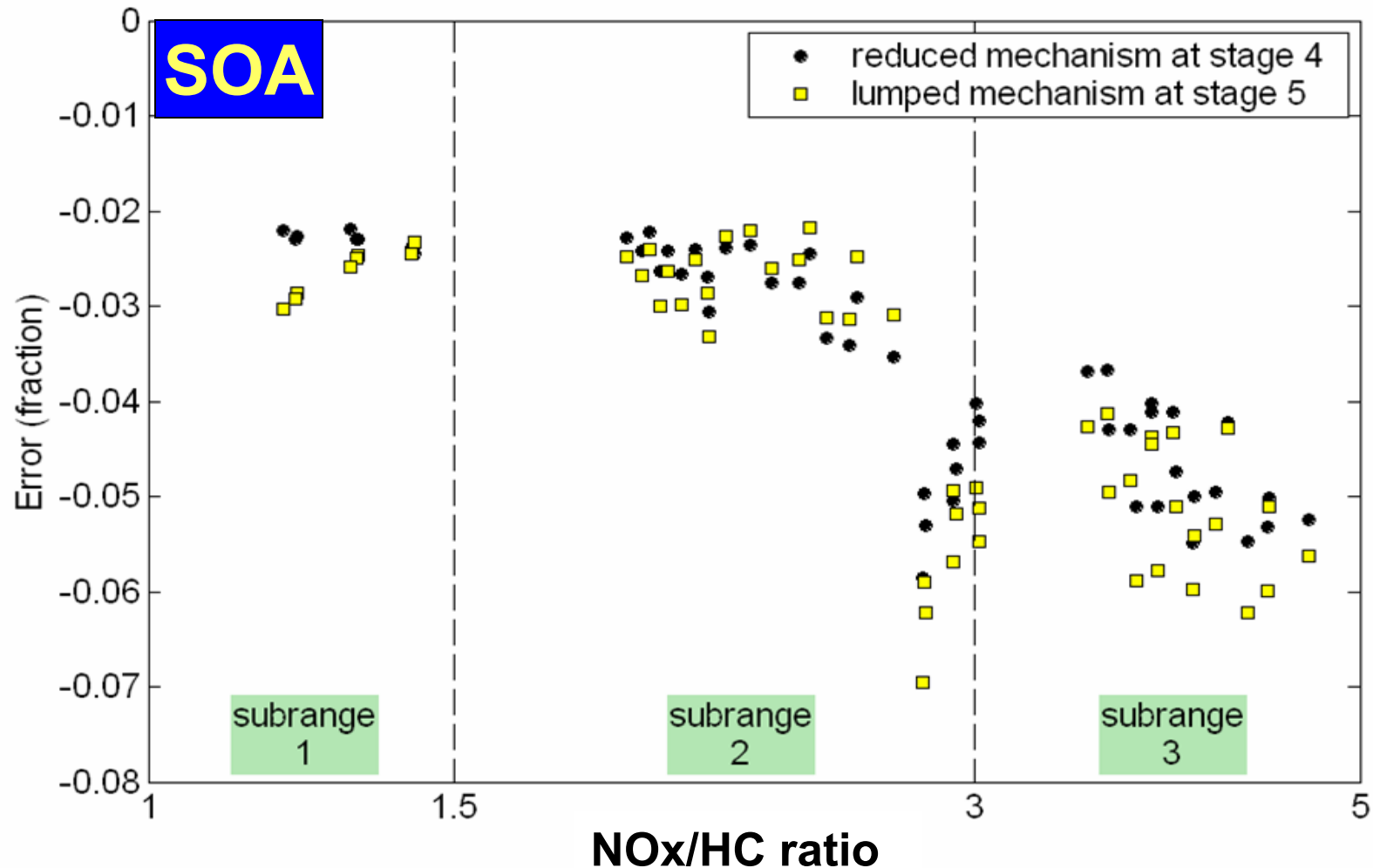


# 5: Fraction is NO<sub>x</sub>/HC dependent

$$X_{\text{each subrange}} = \text{mean}(\text{fractions}_{\text{each subrange}})$$

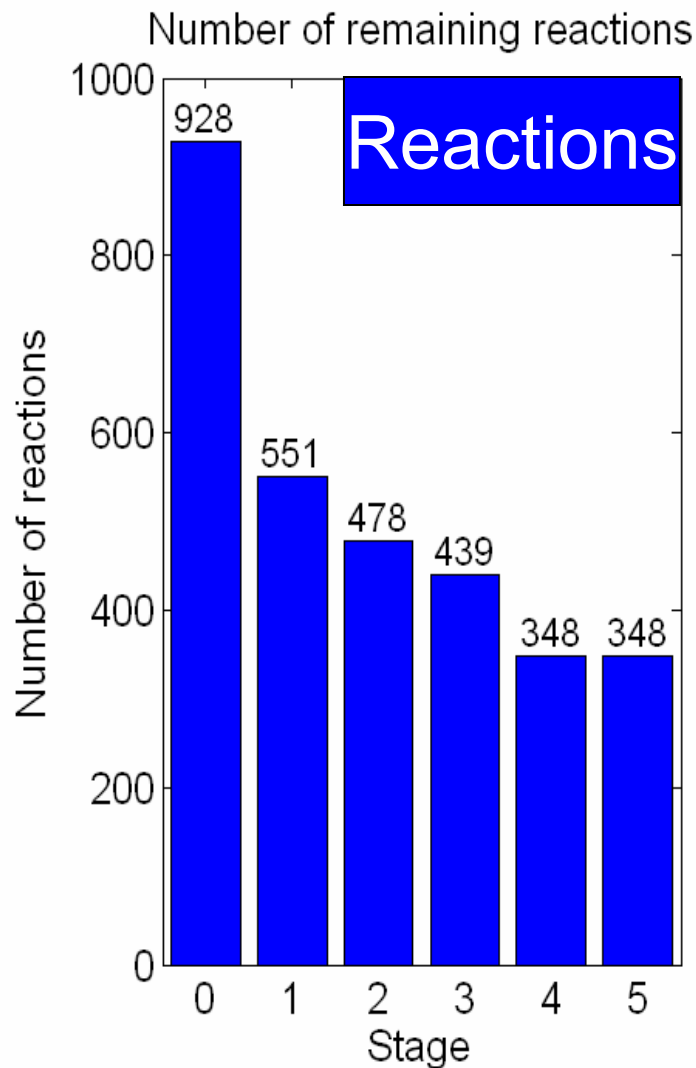
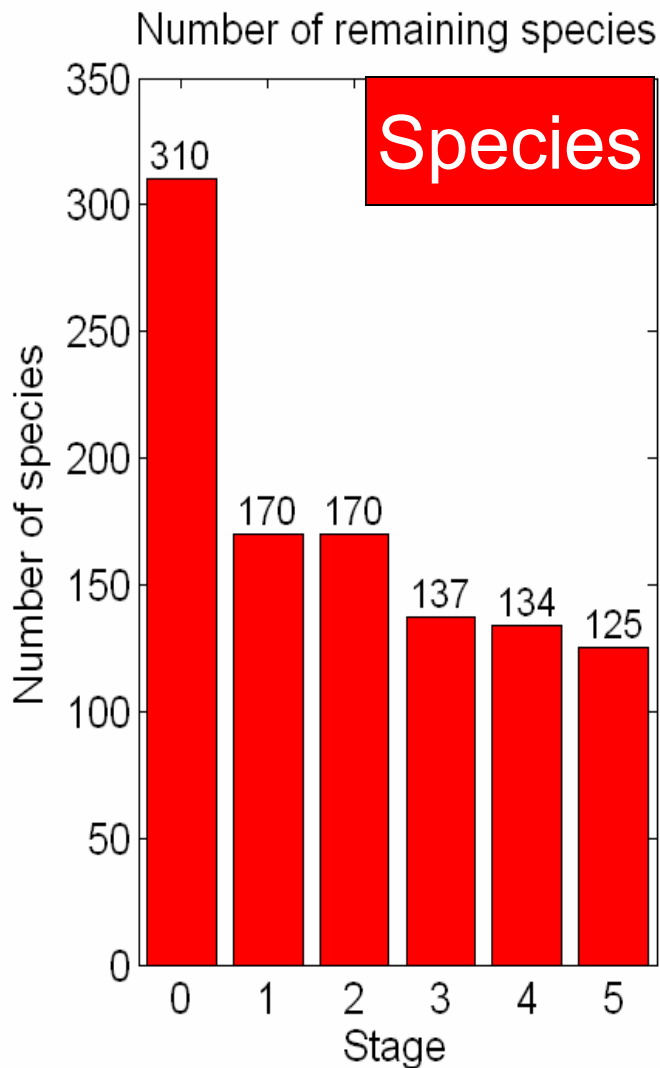


# 5:Lumped Mechanisms at stage 5



16 species have been lumped into 7 groups!

# Summary of model reduction (5)



Stages:

- 0) Full
- 1) DRGEP
- 2) PCA
- 3) QSSA
- 4) ISSA
- 5) Lumping

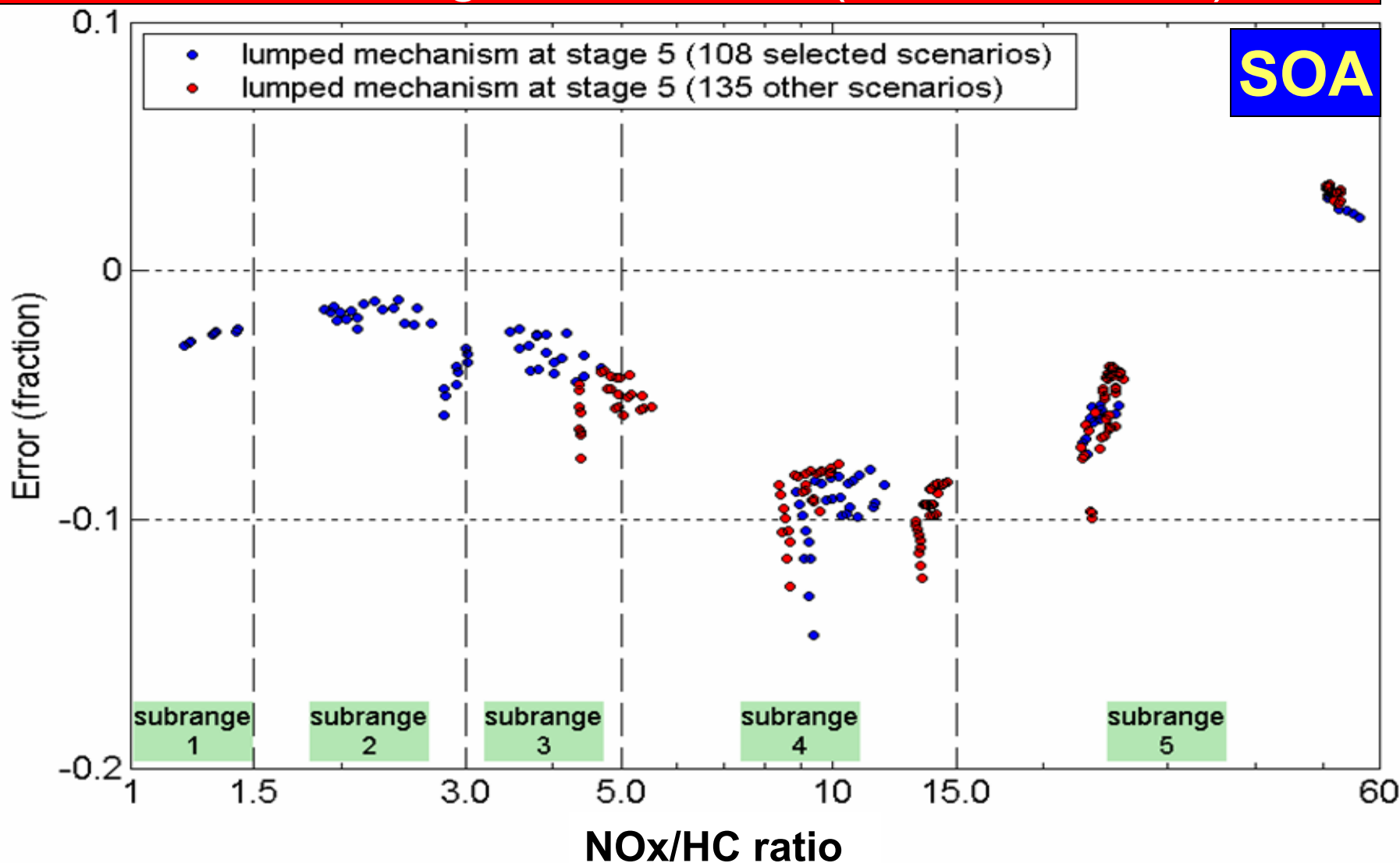
Removed:

Species : 9

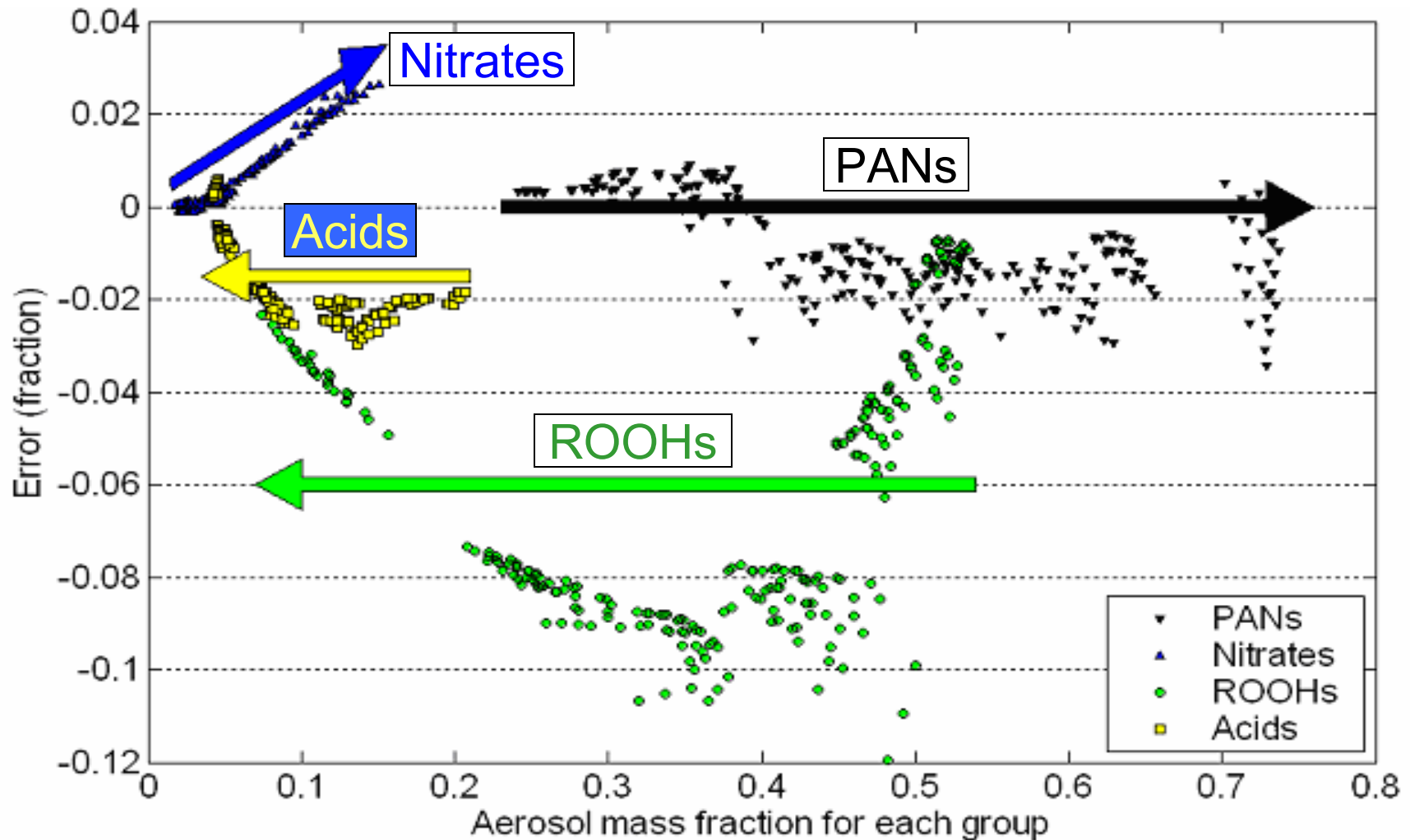
Reactions: 0

# Final evaluation

Reduced mechanism for total SOA formation under a **wider** range of NO<sub>x</sub>/HC (243 scenarios)



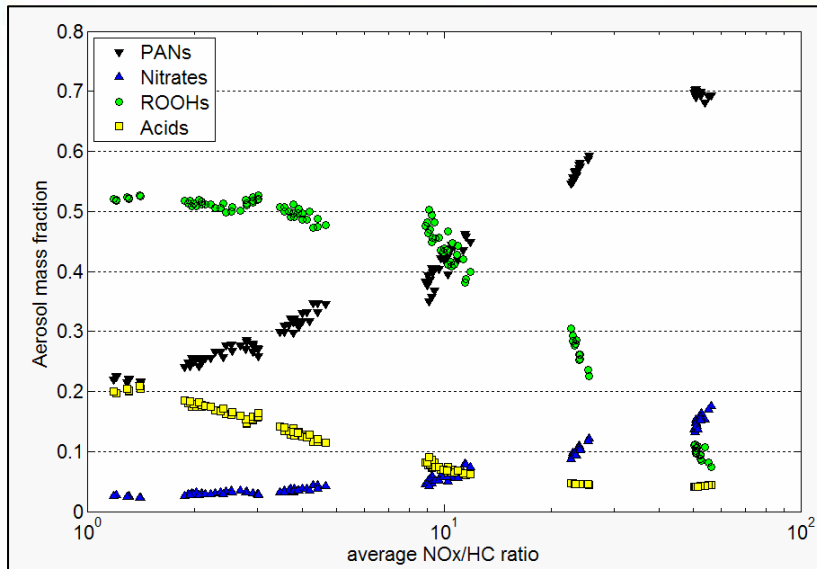
# Final reduced mechanism could describe the SOA formation from each group under a wide range of NO<sub>x</sub>/HC



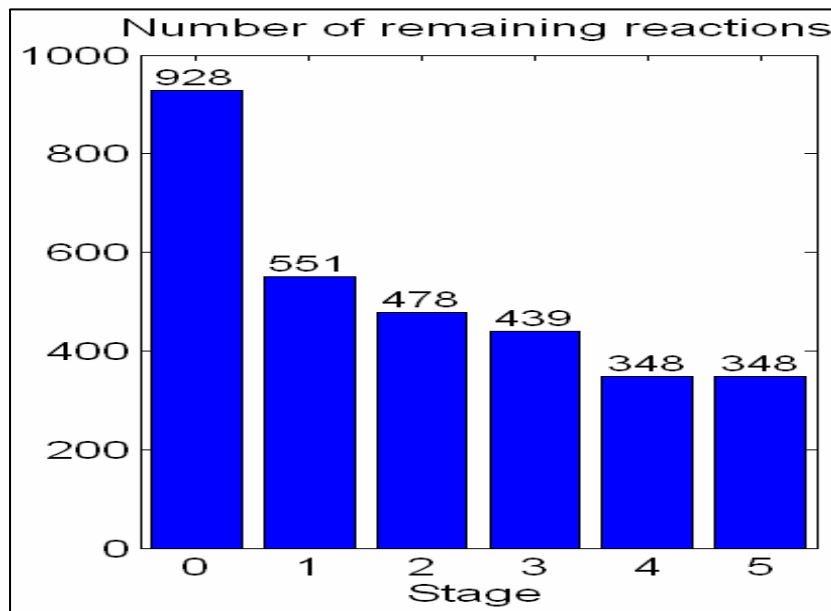
# Summary mechanism reduction

1. A **detailed  $\alpha$ -pinene** oxidation mechanism has been **reduced systematically** by a factor of 2.5.
2. A **new lumping scheme** has been developed and applied to reduce the chemical mechanism.
3. SOA formation is **NO<sub>x</sub>/HC dependent**, therefore, the mechanism reduction is based on the NO<sub>x</sub>/HC (adaptive method).

# Outline



**Part I**  
**Detailed mechanism (MCM)**  
for SOA formation



**Part II**  
**Systematic reduction of**  
the detailed mechanism

# Conclusions

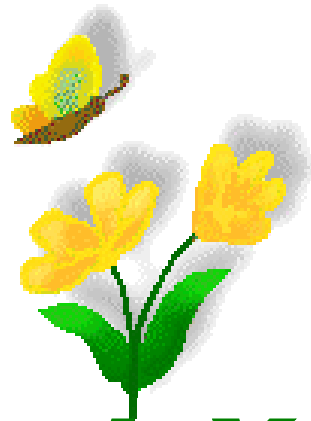
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1. A **detailed chemical mechanism** shows that the **total SOA mass** and the **organic aerosol compositions** are **NO<sub>x</sub>/HC dependent**.
2. **Five systematic mechanism reduction methods** are used to reduce the large chemical mechanism.

# Future studies

## Mechanism reduction

1. **Automatic selection of optimum threshold** at each stage of mechanism reduction
2. Other mechanism reduction techniques.



***Thank You***

**AdAm XiA**

**York University**

**Now at Environment Canada**

**AirQuality@Gmail.com**



***Thank you again !***



**Mechanism reduction**  
**Stage 2 - 4**

# 2: Principal Component Analysis

(Turanyi et al., 1989)

Remove redundant rxns

1. Rate sensitivity matrix  $\mathbf{F}$

$$F_{ij} = \frac{\partial \ln f_i}{\partial \ln k_j} = \frac{\nu_{ij} R_j}{f_i}$$

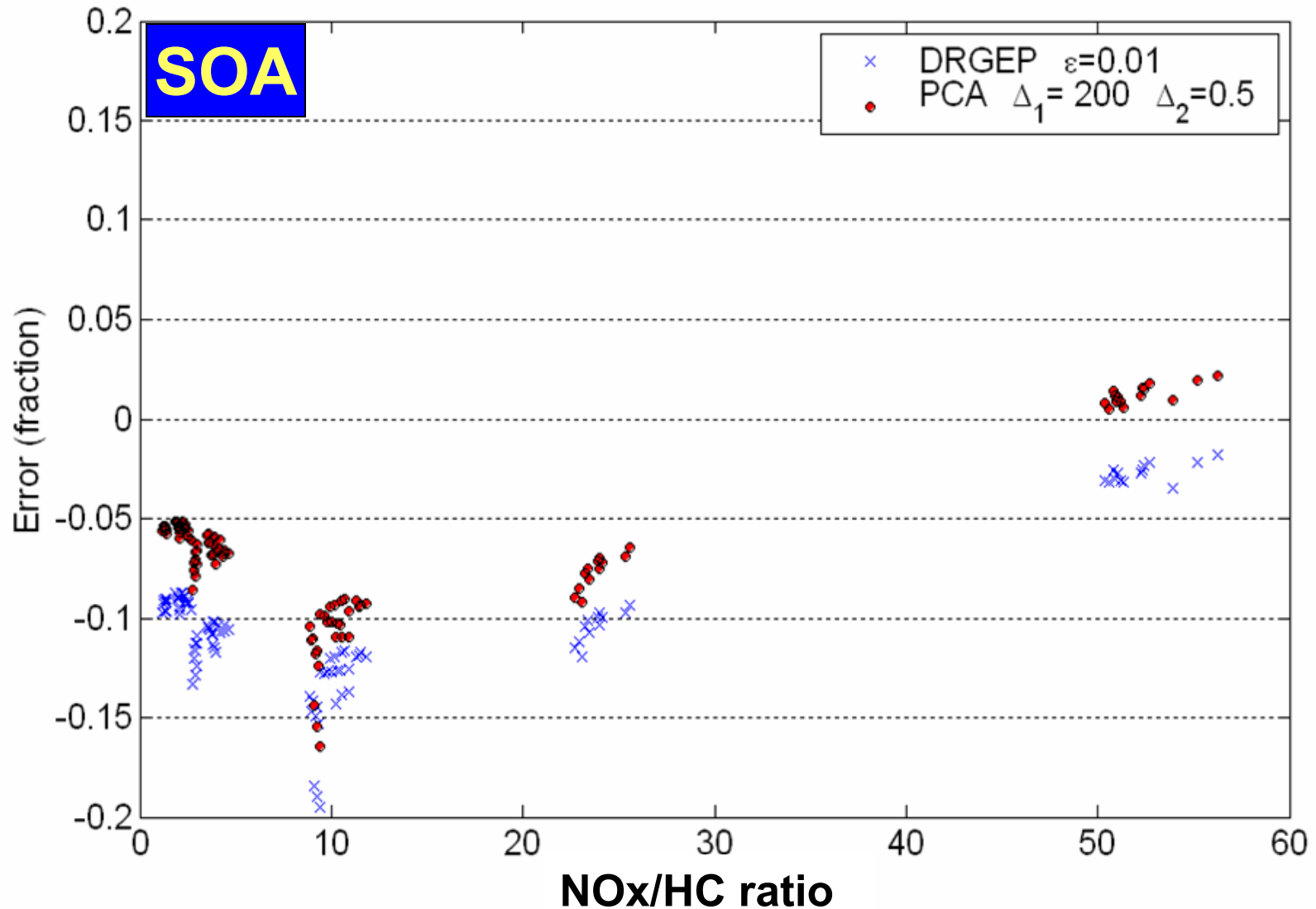
where

$$f_i(\mathbf{c}, \mathbf{k}) = \frac{dc_i}{dt} = - \sum_{j=1}^M \nu_{ij} R_j$$

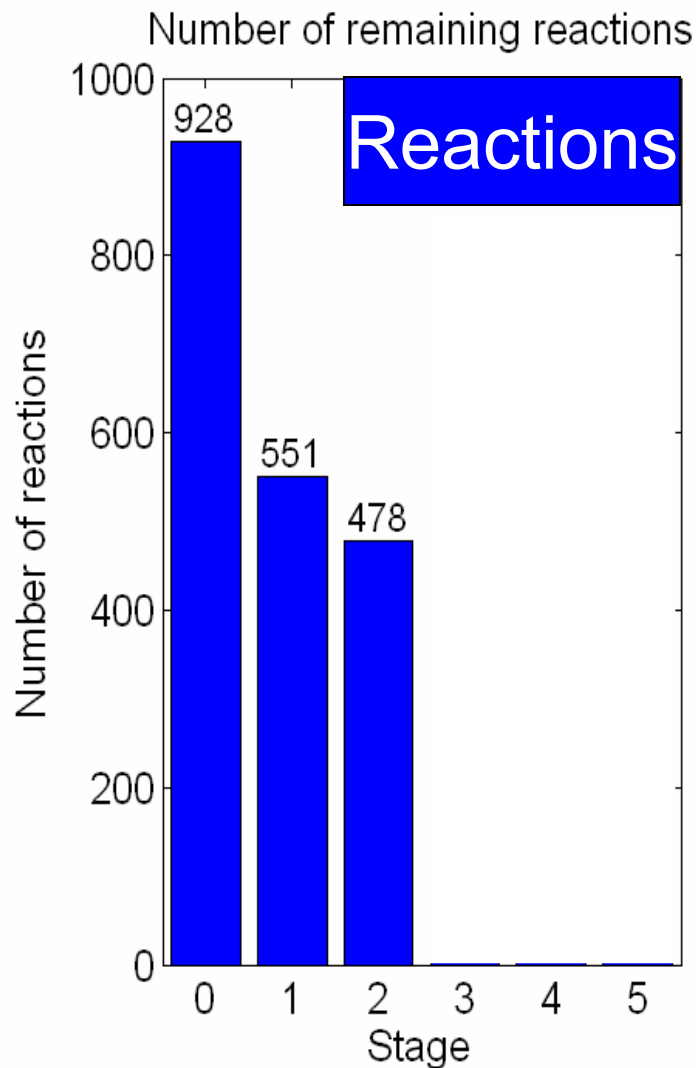
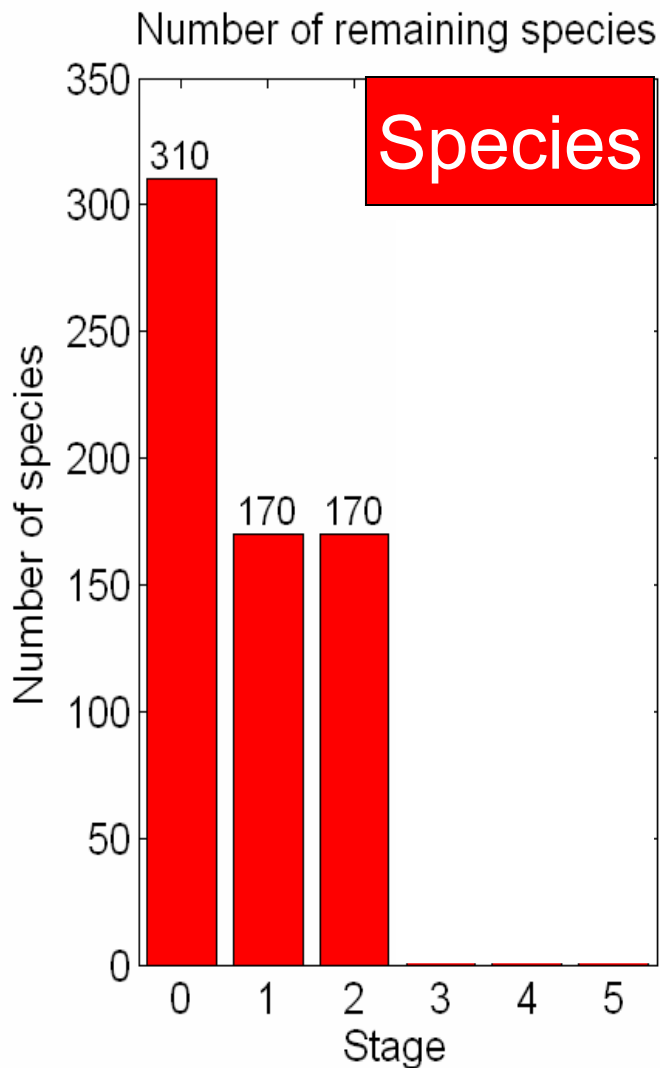
and  $k_j$  = rate constant for the reaction.

2. Principal Component Analysis (PCA) is the eigenvalue-eigenvector decomposition of the matrix  $\mathbf{F}^T \mathbf{F}$ .
3. Reaction, corresponding to a **large eigenvector** and an associated **high eigenvalue**, is an **important reaction**.
4. As a result, 73 out of 551 reactions have been removed. (threshold for the eigenvalue is 200, threshold for the eigenvector is 0.5.)

# 2: Comparison between two stages



# Summary of model reduction (2)



Stages:  
0) Full  
1) DRGEP  
2) PCA

Removed:  
Species : 0  
Reactions: 73

# 3: Quasi-Steady-State species

(Turanyi et al., 1993)

Remove QSS species

1 Species selected as QSS species, based on the instant error  $\left(\frac{\Delta c_i}{c_i}\right)$ , can be removed

$$\frac{\Delta c_i}{c_i} \leq 0.05$$

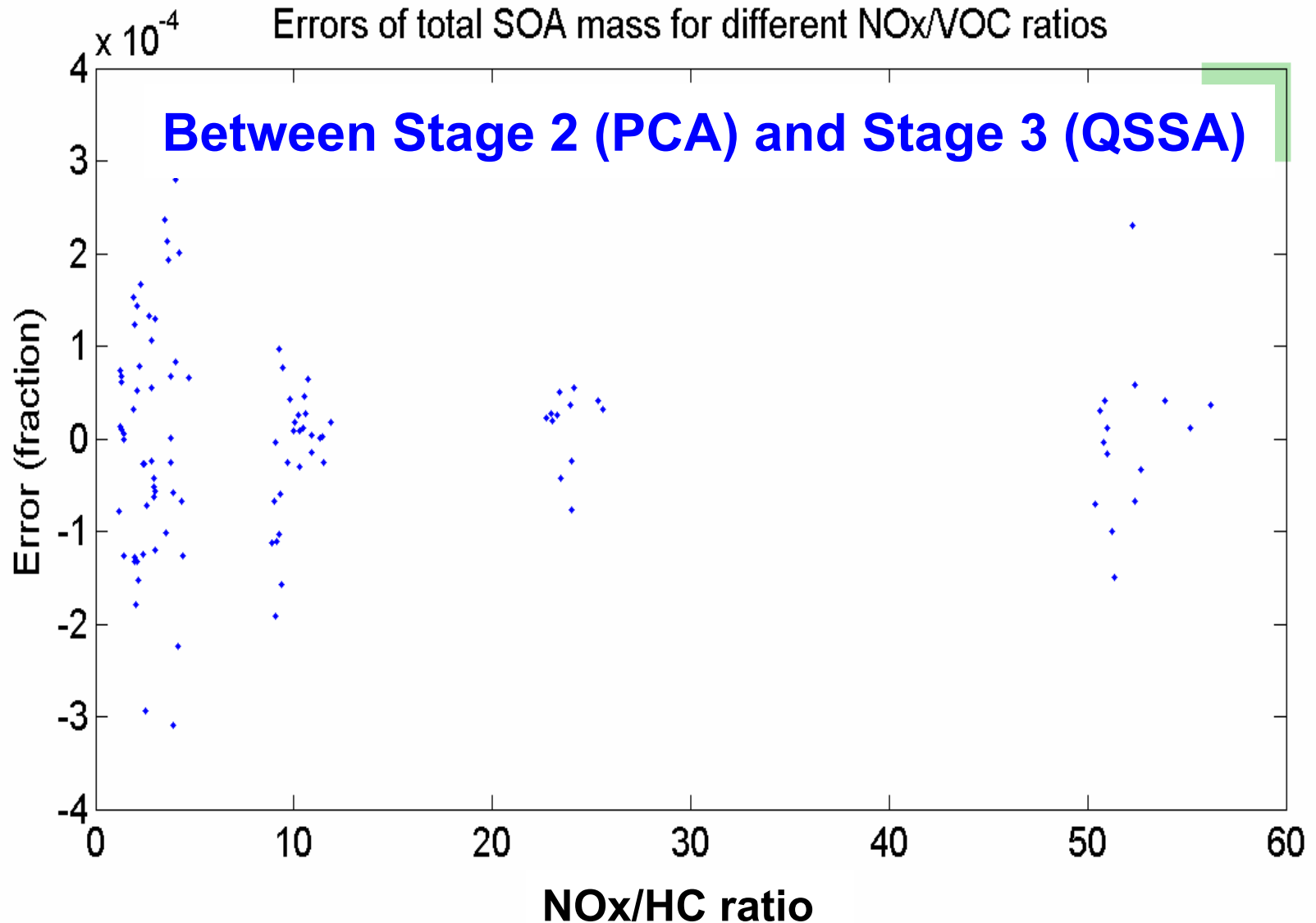
where

$$\Delta c_i = \frac{1}{J_{ii}} \frac{dc_i}{dt}$$

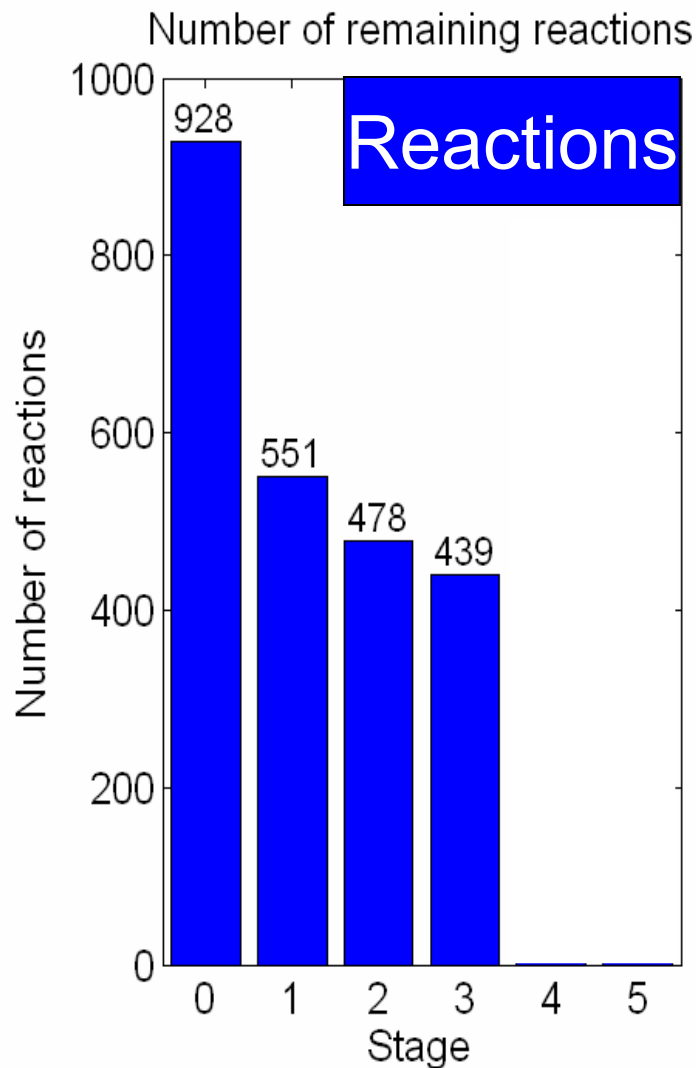
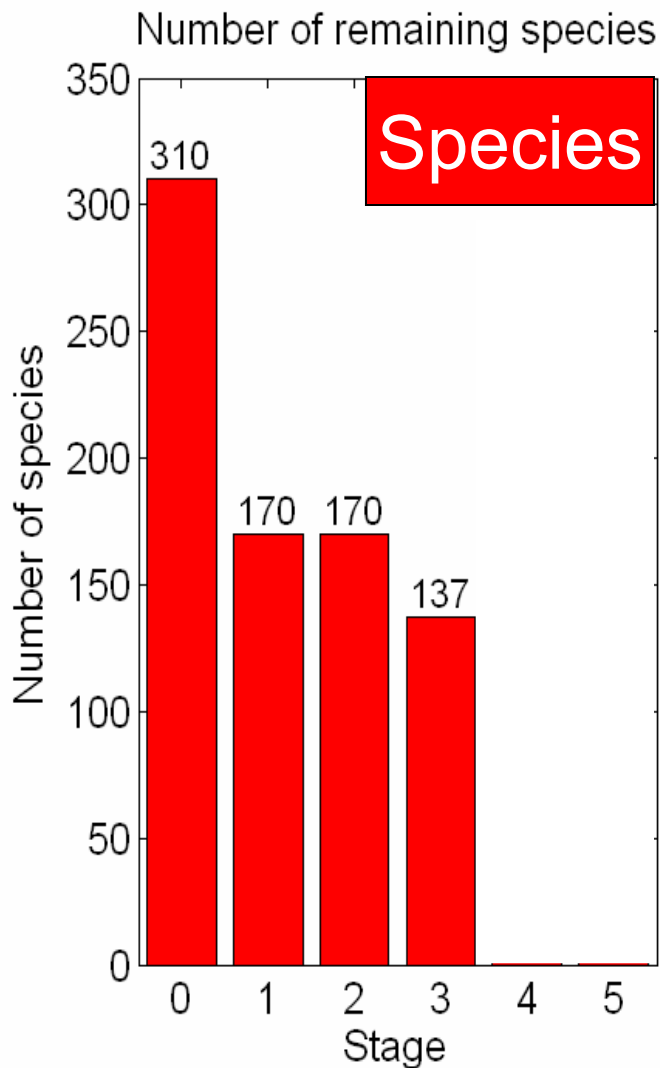
$$J_{ii} = \frac{1}{\delta_{ij}} \frac{\partial}{\partial c_j} \left( \frac{dc_i}{dt} \right)$$

2. As a result of this method, 33 RO species have been removed.

# 3: Quasi-Steady-State species



# Summary of model reduction (3)



Stages:  
0) Full  
1) DRGEP  
2) PCA  
3) **QSSA**

Removed:  
Species : 33  
Reactions: 39

# 4: Iterative screening method (ISSA)

(Mauersberger, 2005)

$$P_i - L_i = \sum_j v_{ij} R_j = \sum_j v_{ij}^+ R_j - \sum_j v_{ij}^- R_j$$

**Production**

$$f_{ij} = \frac{v_{ij}^+ R_j}{P_i}$$

**Loss**

$$g_{ij} = \frac{v_{ij}^- R_j}{L_i}$$

$i$  — species  $i$  (major species)

$j$  —  $j$ th rxn

$R_j$  — reaction rate for the  $j$ th rxn

**1) Major species**

**2) Important rxns**

**3) Species (updated)**

$v_{ij}^+$  — stoich. coeff. for species  $i$  in the  $j$ th rxn as a **product**

$f_{ij}$  — relative importance of the  $j$ th rxn to the **production term** ( $P_i$ ) for species  $i$

$v_{ij}^-$  — stoich. coeff. for species  $i$  in the  $j$ th rxn as a **reactant**

$g_{ij}$  — relative importance of the  $j$ th rxn to the **loss term** ( $L_i$ ) for species  $i$

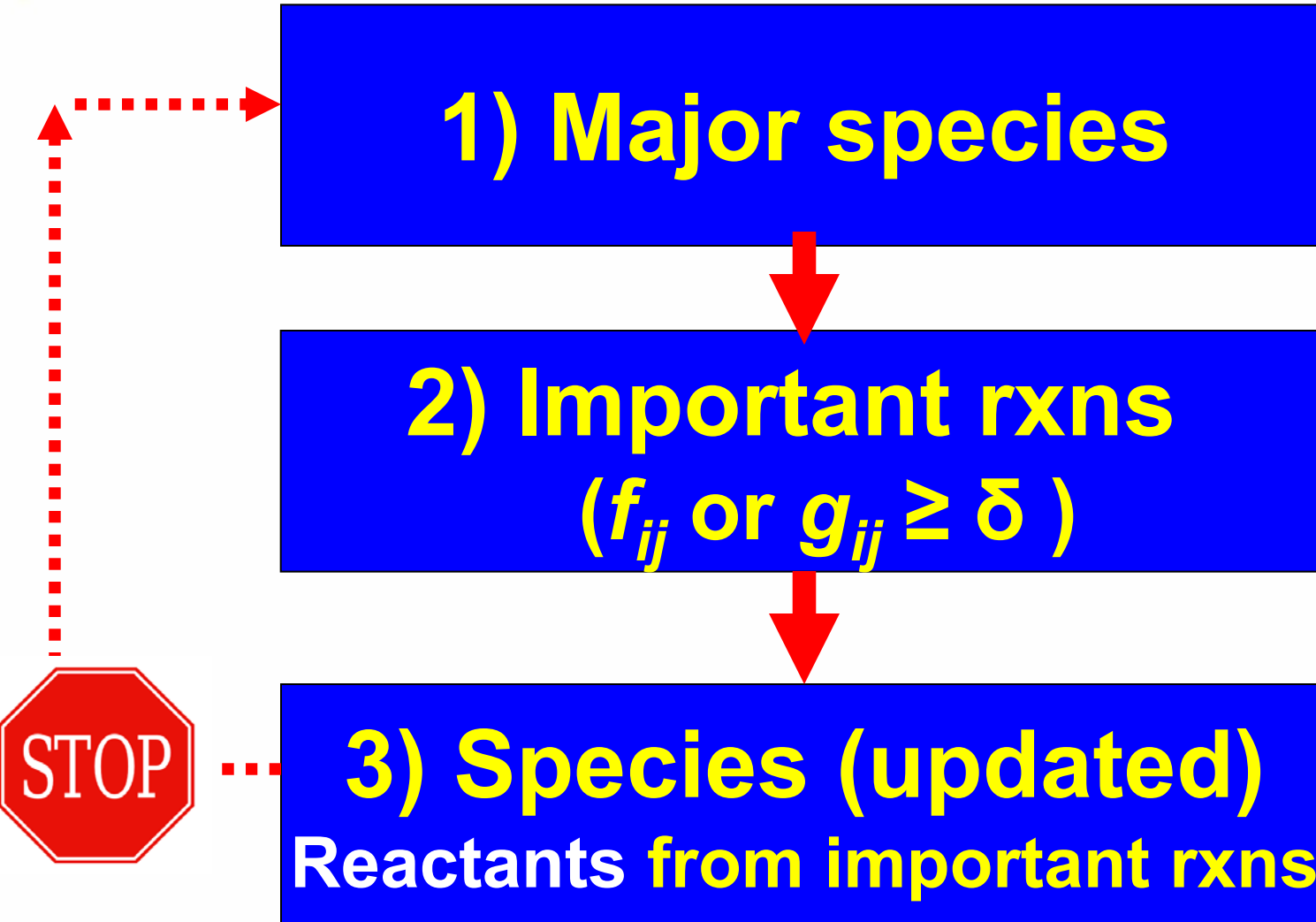
## 4: Procedure to find “*major species*” and “*important reactions*” by using ISSA

**1) Major species**

**2) Important rxns**  
( $f_{ij}$  or  $g_{ij} \geq \delta$ )

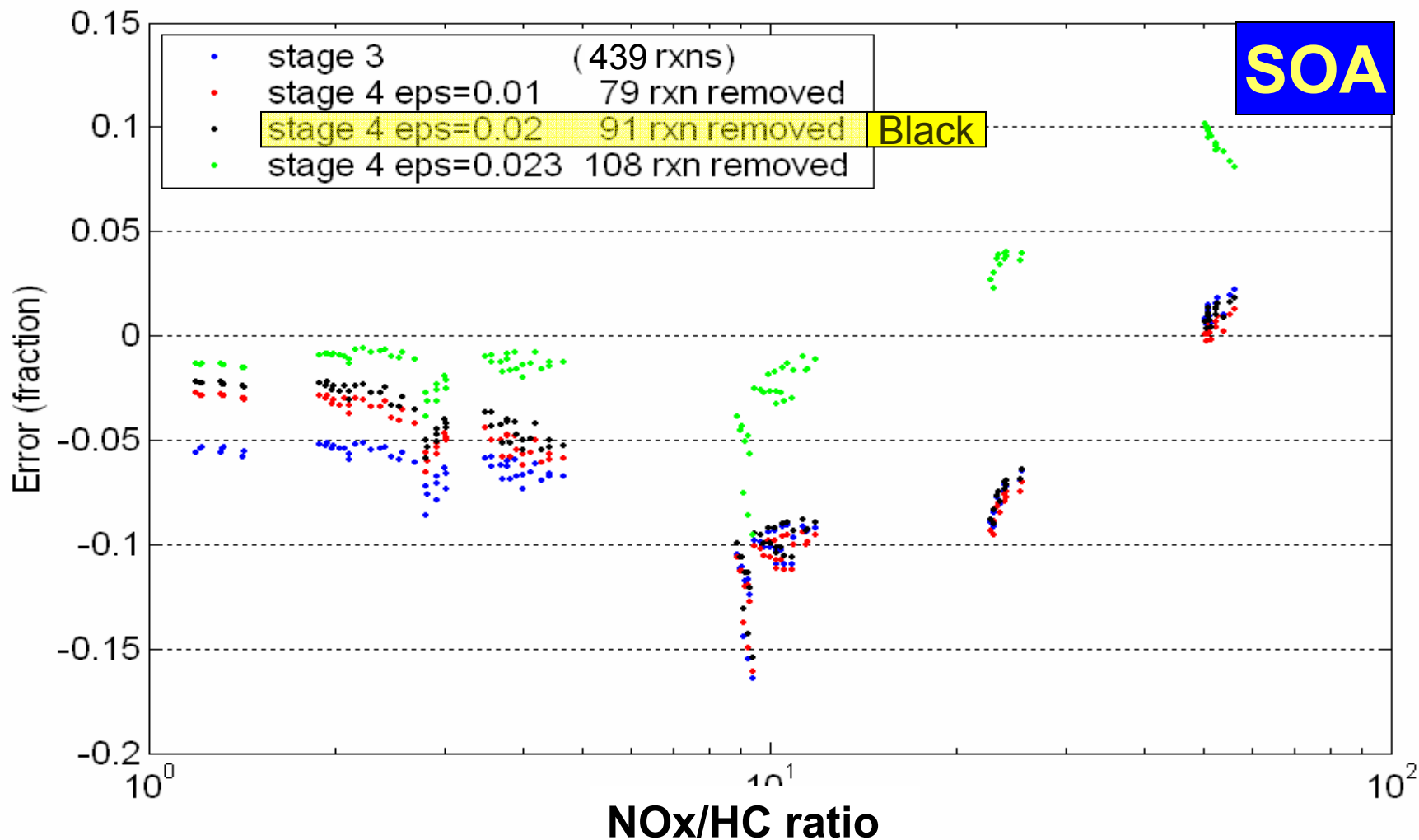
**3) Species (updated)**  
Reactants from important rxns

STOP

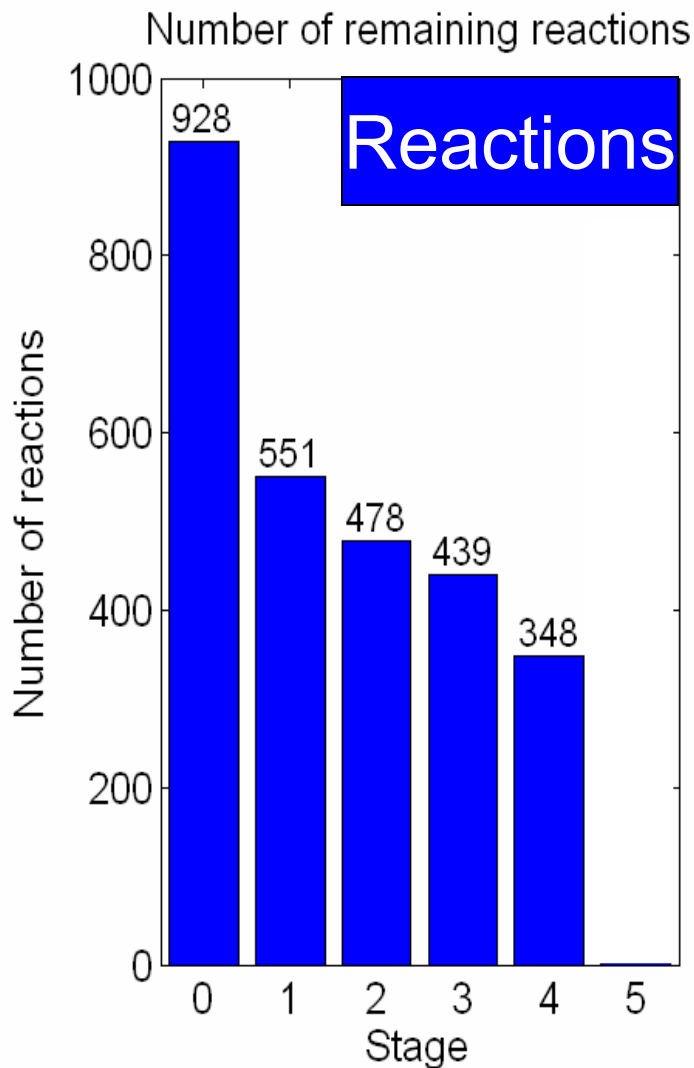
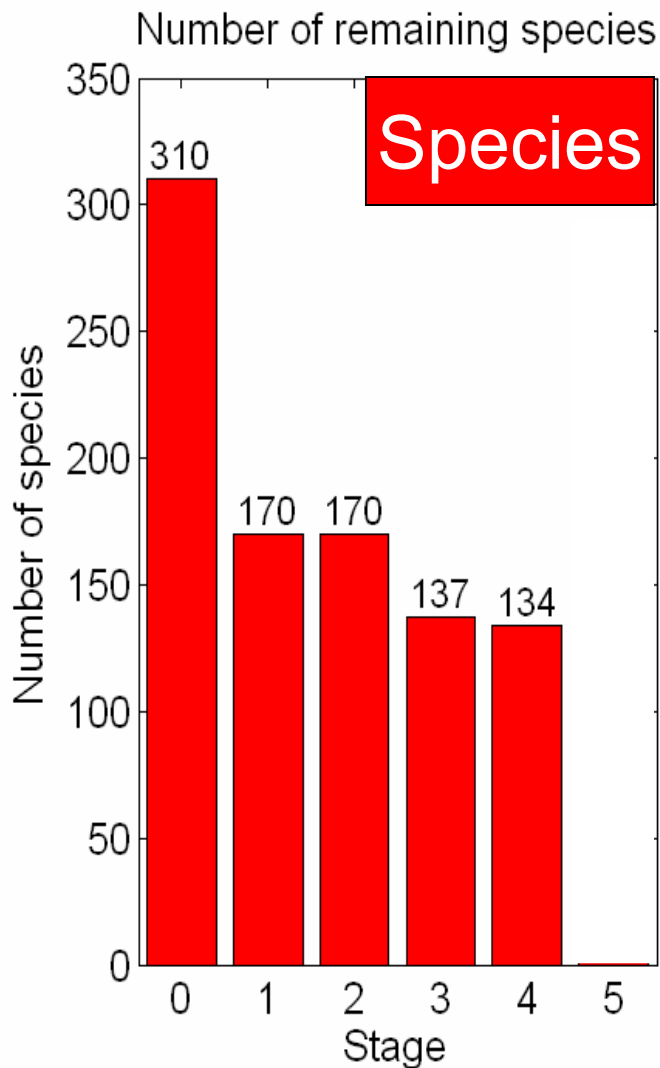


# 4: Evaluation of the ISSA method

Reduced mechanism is very sensitive to the selection of the threshold



# Summary of model reduction (4)



Stages:  
0) Full  
1) DRGEP  
2) PCA  
3) QSSA  
4) ISSA

Removed:  
Species : 3  
Reactions: 91

